
matrix_decomposition Documentation

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Several functions are included in this package. The most important are summarized here.

1.1 decompose a matrix

`matrix.decompose` (*A*, *permutation_method*=None, *check_finite*=True, *return_type*=None)
Computes a decomposition of a matrix.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Matrix to be decomposed. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **permutation_method** (*str*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in `matrix.PERMUTATION_METHODS`. If A is sparse, it can also be a value in `matrix.SPARSE_PERMUTATION_METHODS`. optional, default: no permutation
- **check_finite** (*bool*) – Whether to check that the input matrix contains only finite numbers. Disabling may result in problems (crashes, non-termination) if the inputs do contain infinities or NaNs. (disabling may improve performance) optional, default: True
- **return_type** (*str*) – The type of the decomposition that should be calculated. It has to be a value in `matrix.DECOMPOSITION_TYPES`. If *return_type* is None the type of the returned decomposition is chosen by the function itself. optional, default: the type of the decomposition is chosen by the function itself

Returns A decomposition of A of type *return_type*.

Return type `matrix.decompositions.DecompositionBase`

Raises `matrix.errors.MatrixNoDecompositionPossibleError` – If the decomposition of A is not possible.

`matrix.PERMUTATION_METHODS` = (None, '', 'none', 'natural', 'decreasing_diagonal_values', '...')
Supported permutation methods for dense and sparse matrices.

```
matrix.SPARSE_PERMUTATION_METHODS = ()
```

Supported permutation methods only for sparse matrices.

```
matrix.DECOMPOSITION_TYPES = ('LDL', 'LDL_compressed', 'LL')
```

Supported types of decompositions.

1.2 examine positive definiteness

```
matrix.is_positive_semi_definite(A)
```

Checks if the passed matrix is positive semi-definite.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.

Returns Whether A is positive semi-definite.

Return type *bool*

```
matrix.is_positive_definite(A)
```

Checks if the passed matrix is positive definite.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.

Returns Whether A is positive definite.

Return type *bool*

1.3 approximate by a decomposition

```
matrix.approximate(A, t=None, min_diag_value=None, max_diag_value=None,
                   min_abs_value=None, permutation_method=None, check_finite=True, re-
                   turn_type=None, callback=None)
```

Computes an approximative decomposition of a matrix.

If A is decomposable in a decomposition of type *return_type*, this decomposition is returned. Otherwise a decomposition of type *return_type* is returned which represents an approximation of A.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be approximated by a decomposition. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **t** (*numpy.ndarray*) – The targeted vector used for the approximation. For each i in range(M) *min_diag_value* <= *t[i]* <= *max_diag_value* must hold. *t* and A must have the same length. optional, default : The diagonal of A is used as *t*.
- **min_diag_value** (*float*) – Each component of the diagonal of the matrix *D* in an returned *LDL* decomposition is forced to be greater or equal to *min_diag_value*. optional, default : 0.
- **max_diag_value** (*float*) – Each component of the diagonal of the matrix *D* in an returned *LDL* decomposition is forced to be lower or equal to *max_diag_value*. optional, default : No maximal value is forced.
- **min_abs_value** (*float*) – Absolute values below *min_abs_value* are considered as zero. optional, default : The resolution of the underlying data type is used.

- **permutation_method** (*str*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in `matrix.PERMUTATION_METHODS`. If *A* is sparse, it can also be a value in `matrix.SPARSE_PERMUTATION_METHODS`. optional, default: No permutation is done.
- **check_finite** (*bool*) – Whether to check that the input matrix contains only finite numbers. Disabling may result in problems (crashes, non-termination) if the inputs do contain infinities or NaNs. (disabling may improve performance) optional, default: True
- **return_type** (*str*) – The type of the decomposition that should be calculated. It has to be a value in `matrix.DECOMPOSITION_TYPES`. optional, default : The type of the decomposition is chosen by the function itself.
- **callback** (*callable*) – In each iteration `callback(i, r)` is called where *i* is the index of the row and column where components of *A* are reduced by the factor *r*. optional, default : No callback function is called.

Returns An approximative decomposition of *A* of type *return_type*.

Return type `matrix.decompositions.DecompositionBase`

Matrix decompositions

Several matrix decompositions are supported. They are available in *matrix.decompositions*:

2.1 LL decomposition

class `matrix.decompositions.LL_Decomposition` (*L=None, p=None*)

Bases: `matrix.decompositions.DecompositionBase`

A matrix decomposition where LL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. This decomposition is also called Cholesky decomposition.

Parameters

- **L** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix L of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (`numpy.ndarray`) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

L

`numpy.matrix` or `scipy.sparse.spmatrix` – The matrix L of the decomposition.

P

`scipy.sparse.dok_matrix` – The permutation matrix. $P @ A @ P.H$ is the matrix A permuted by the permutation of the decomposition

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

decomposition_type

`str` – The type of this decomposition.

is_permuted

`bool` – Whether this is a decomposition with permutation.

is_positive_definite()

`bool`: Whether the matrix represented by this decomposition is positive definite.

is_positive_semi_definite()

`bool`: Whether the matrix represented by this decomposition is positive semi-definite.

is_sparse

`bool` – Whether this is a sparse decomposition.

is_type(*decomposition_type*)

Whether this is a decomposition of the passed type.

Parameters **decomposition_type** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(*directory_name*, *filename_prefix=None*)

Loads a decomposition of this type.

Parameters

- **directory_name** (*str*) – A directory where this decomposition is saved.
- **filename_prefix** (*str*) – A prefix for the filenames of the attributes of this decomposition.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. $A[p[:, \text{np.newaxis}], p[\text{np.newaxis}, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix(*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save(*directory_name*, *filename_prefix=None*)

Saves this decomposition.

Parameters

- **directory_name** (*str*) – A directory where this decomposition should be saved.
- **filename_prefix** (*str*) – A prefix for the filenames of the attributes of this decomposition.

to (*decomposition_type*, *copy=False*)
Convert decomposition to passed type.

Parameters

- **decomposition_type** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *decomposition_type*, a decomposition of type *decomposition_type* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

to_LDL_Decomposition ()

to_any (**decomposition_types*, *copy=False*)
Convert decomposition to any of the passed types.

Parameters

- ***decomposition_types** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *decomposition_types*, a decomposition of type *decomposition_type[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

unpermute_matrix (*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

2.2 LDL decomposition

class *matrix.decompositions.LDL_Decomposition* (*L=None*, *d=None*, *p=None*)

Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. *D* is a diagonal matrix. Only the diagonal values of *D* are stored.

Parameters

- **L** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix L of the decomposition. optional, If it is not set yet, it must be set later.
- **d** (*numpy.ndarray*) – The vector of the diagonal components of D of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

D
scipy.sparse.dia_matrix – The permutation matrix.

L
numpy.matrix or *scipy.sparse.spmatrix* – The matrix L of the decomposition.

LD
numpy.matrix or *scipy.sparse.spmatrix* – A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

P
scipy.sparse.dok_matrix – The permutation matrix. $P @ A @ P.H$ is the matrix A permuted by the permutation of the decomposition

composed_matrix
numpy.matrix or *scipy.sparse.spmatrix* – The composed matrix represented by this decomposition.

copy()
Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

d
numpy.ndarray – The diagonal vector of the matrix D of the decomposition.

decomposition_type
str – The type of this decomposition.

is_permuted
bool – Whether this is a decomposition with permutation.

is_positive_definite()
bool: Whether the matrix represented by this decomposition is positive definite.

is_positive_semi_definite()
bool: Whether the matrix represented by this decomposition is positive semi-definite.

is_sparse
bool – Whether this is a sparse decomposition.

is_type(decomposition_type)
Whether this is a decomposition of the passed type.

Parameters **decomposition_type** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type *bool*

load (*directory_name*, *filename_prefix*=None)

Loads a decomposition of this type.

Parameters

- **directory_name** (*str*) – A directory where this decomposition is saved.
- **filename_prefix** (*str*) – A prefix for the filenames of the attributes of this decomposition.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. `A[p[:, np.newaxis], p[np.newaxis, :]]` is the matrix `A` permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix (*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix `A` permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*directory_name*, *filename_prefix*=None)

Saves this decomposition.

Parameters

- **directory_name** (*str*) – A directory where this decomposition should be saved.
- **filename_prefix** (*str*) – A prefix for the filenames of the attributes of this decomposition.

to (*decomposition_type*, *copy*=False)

Convert decomposition to passed type.

Parameters

- **decomposition_type** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *decomposition_type*, a decomposition of type *decomposition_type* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

to_LDL_DecompositionCompressed ()

to_LL_Decomposition ()

to_any (**decomposition_types*, *copy*=False)

Convert decomposition to any of the passed types.

Parameters

- ***decomposition_types** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *decomposition_types*, a decomposition of type *decomposition_type[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

unpermute_matrix (*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

2.3 LDL decomposition compressed

class *matrix.decompositions.LDL_DecompositionCompressed* (*LD=None, p=None*)

Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. *D* is a diagonal matrix. *L* and *D* are stored in one matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*.

Parameters

- **LD** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – A matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where *A* is a matrix. optional, default: no permutation

D

scipy.sparse.dia_matrix – The permutation matrix.

L

numpy.matrix or *scipy.sparse.spmatrix* – The matrix *L* of the decomposition.

LD

numpy.matrix or *scipy.sparse.spmatrix* – A matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*.

P

scipy.sparse.dok_matrix – The permutation matrix. $P @ A @ P.H$ is the matrix *A* permuted by the permutation of the decomposition

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

d

`numpy.ndarray` – The diagonal vector of the matrix D of the decomposition.

decomposition_type

`str` – The type of this decomposition.

is_permuted

`bool` – Whether this is a decomposition with permutation.

is_positive_definite()

`bool`: Whether the matrix represented by this decomposition is positive definite.

is_positive_semi_definite()

`bool`: Whether the matrix represented by this decomposition is positive semi-definite.

is_sparse

`bool` – Whether this is a sparse decomposition.

is_type(decomposition_type)

Whether this is a decomposition of the passed type.

Parameters `decomposition_type` (`str`) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(directory_name, filename_prefix=None)

Loads a decomposition of this type.

Parameters

- **directory_name** (`str`) – A directory where this decomposition is saved.
- **filename_prefix** (`str`) – A prefix for the filenames of the attributes of this decomposition.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. $A[p[:, \text{np.newaxis}], p[\text{np.newaxis}, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix(A)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

save (*directory_name*, *filename_prefix=None*)

Saves this decomposition.

Parameters

- **directory_name** (*str*) – A directory where this decomposition should be saved.
- **filename_prefix** (*str*) – A prefix for the filenames of the attributes of this decomposition.

to (*decomposition_type*, *copy=False*)

Convert decomposition to passed type.

Parameters

- **decomposition_type** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *decomposition_type*, a decomposition of type *decomposition_type* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

to_LDL_Decomposition ()

to_any (**decomposition_types*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***decomposition_types** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *decomposition_types*, a decomposition of type *decomposition_type[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

unpermute_matrix (*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

2.4 base decomposition

class `matrix.decompositions.DecompositionBase` (*p=None*)

Bases: `object`

A matrix decomposition.

This class is a base class for matrix decompositions.

Parameters *p* (`numpy.ndarray`) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, \text{np.newaxis}], p[\text{np.newaxis}, :]]$ where A is a matrix. optional, default: no permutation

P

`scipy.sparse.dok_matrix` – The permutation matrix. $P @ A @ P.H$ is the matrix A permuted by the permutation of the decomposition

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

decomposition_type

`str` – The type of this decomposition.

is_permuted

`bool` – Whether this is a decomposition with permutation.

is_positive_definite

`bool` – Whether the matrix represented by this decomposition is positive definite.

is_positive_semi_definite

`bool` – Whether the matrix represented by this decomposition is positive semi-definite.

is_sparse

`bool` – Whether this is a sparse decomposition.

is_type (*decomposition_type*)

Whether this is a decomposition of the passed type.

Parameters *decomposition_type* (`str`) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load (*directory_name*, *filename_prefix=None*)

Loads a decomposition of this type.

Parameters

- **directory_name** (`str`) – A directory where this decomposition is saved.
- **filename_prefix** (`str`) – A prefix for the filenames of the attributes of this decomposition.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

n
`int` – The dimension of the squared decomposed matrix.

P
`numpy.ndarray` – The permutation vector. `A[p[:, np.newaxis], p[np.newaxis, :]]` is the matrix `A` permuted by the permutation of the decomposition

p_inverse
`numpy.ndarray` – The permutation vector that undos the permutation.

permute_matrix(*A*)
Permute a matrix by the permutation of the decomposition.

Parameters *A* (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*directory_name*, *filename_prefix*=None)
Saves this decomposition.

Parameters

- **directory_name** (`str`) – A directory where this decomposition should be saved.
- **filename_prefix** (`str`) – A prefix for the filenames of the attributes of this decomposition.

to (*decomposition_type*, *copy*=False)
Convert decomposition to passed type.

Parameters

- **decomposition_type** (`str`) – The decomposition type to which this decomposition is converted.
- **copy** (`bool`) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *decomposition_type*, a decomposition of type *decomposition_type* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

to_any (**decomposition_types*, *copy*=False)
Convert decomposition to any of the passed types.

Parameters

- ***decomposition_types** (`str`) – The decomposition types to any of them this this decomposition is converted.
- **copy** (`bool`) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *decomposition_types*, a decomposition of type *decomposition_type*[0] is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

unpermute_matrix(*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

This is an overview about the exceptions that could arise in this package. They are available in *matrix.errors*:

3.1 MatrixNoDecompositionPossibleError

```
class matrix.errors.MatrixNoDecompositionPossibleError (matrix=None,    decomp-
                                                    sition_decription=None,
                                                    message=None)
```

Bases: *matrix.errors.MatrixError*

The matrix decomposition is not possible for this matrix.

3.2 MatrixNoLDLDecompositionPossibleError

```
class matrix.errors.MatrixNoLDLDecompositionPossibleError (matrix=None, problem-
                                                    atic_leading_principal_submatrix_index=None,
                                                    subdecomposi-
                                                    tion=None)
```

Bases: *matrix.errors.MatrixNoDecompositionPossibleWithProblematicSubdecompositionError*

A LDL decomposition is not possible for this matrix.

3.3 MatrixNoLLDecompositionPossibleError

```
class matrix.errors.MatrixNoLLDecompositionPossibleError (matrix=None, problem-
                                                    atic_leading_principal_submatrix_index=None,
                                                    subdecomposi-
                                                    tion=None)
```

Bases: *matrix.errors.MatrixNoDecompositionPossibleWithProblematicSubdecompositionError*

A LL decomposition is not possible for this matrix.

3.4 MatrixDecompositionNoConversionImplementedError

```
class matrix.errors.MatrixDecompositionNoConversionImplementedError (original_decomposition=None,  
                                                                    de-  
                                                                    sired_decomposition_type=None)
```

Bases: `matrix.errors.MatrixError`

A decomposition conversion is not implemented for this type.

3.5 MatrixNoDecompositionPossibleWithProblematicSubdecompositionError

```
class matrix.errors.MatrixNoDecompositionPossibleWithProblematicSubdecompositionError (matrix=  
de-  
com-  
po-  
si-  
tion_d  
prob-  
lem-  
atic_le  
sub-  
de-  
com-  
po-  
si-  
tion=N
```

Bases: `matrix.errors.MatrixNoDecompositionPossibleError`

The desired matrix decomposition is not possible for this matrix. Only a subdecomposition could be calculated

3.6 MatrixError

```
class matrix.errors.MatrixError (matrix=None, message=None)
```

Bases: `Exception`

An exception related to a matrix.

This is the base exception for all exceptions in this package.

4.1 v0.6

- decompositions are now saveable and loadable

4.2 v0.5

- matrices can now be approximated by decompositions

4.3 v0.4

- matrices can now be examined if they are positive definite or positive semi-definite

4.4 v0.3

- dense and sparse matrices are now decomposable into several types (LL, LDL, LDL compressed)

4.5 v0.2

- decompositons are now convertible to other decompositon types
- decompositions are now comparable

4.6 v0.1

- several decompositions types added (LL, LDL, LDL compressed)
- permutation capabilities added

CHAPTER 5

Indices and tables

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