matrix_decomposition Documentation

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Contents

This is *matrix-decomposition*, a library for decompose (factorize) dense and sparse matrices in Python.

CHAPTER 1

Release info

There are several ways to obtain and install this package.

1.1 Conda

To install this package with *conda* run:

```
conda install -c jore matrix-decomposition
```

https://anaconda.org/jore/matrix-decomposition

1.2 pip

To install this package with *pip* run:

```
pip install 'matrix-decomposition'
```

https://pypi.python.org/pypi/matrix-decomposition

1.3 GitHub

To clone this package with *git* run:

```
git clone https://github.com/jor-/matrix-decomposition.git
```

To install this package after that with *python* run:

```
cd matrix-decomposition; python setup.py install
```

https://github.com/jor-/matrix-decomposition

CHAPTER 2

Documentation

https://matrix-decomposition.readthedocs.io

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4.1 Functions

Several functions are included in this package. The most important are summarized here.

4.1.1 decompose a matrix

matrix.**decompose**(*A*, *permutation=None*, *return_type=None*, *check_finite=True*, *overwrite_A=False*)

Computes a decomposition of a matrix.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – Matrix to be decomposed. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **permutation** (*str or numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.UNIVERSAL_PERMUTATION_METHODS*. If *A* is sparse, it can also be a value in *matrix.SPARSE_ONLY_PERMUTATION_METHODS*. It is also possible to directly pass a permutation vector. optional, default: no permutation
- **return_type** (*str*) – The type of the decomposition that should be calculated. It has to be a value in *matrix.DECOMPOSITION_TYPES*. If return_type is None the type of the returned decomposition is chosen by the function itself. optional, default: the type of the decomposition is chosen by the function itself
- **check_finite** (*bool*) – Whether to check that the input matrix contains only finite numbers. Disabling may result in problems (crashes, non-termination) if the inputs do contain infinities or NaNs. Disabling gives a performance gain. optional, default: True
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A. Enabling may result in performance gain. optional, default: False

Returns A decomposition of *A* of type *return_type*.

Return type *matrix.decompositions.DecompositionBase*

Raises

- *matrix.errors.NoDecompositionPossibleError* – If the decomposition of *A* is not possible.
- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.

matrix.**UNIVERSAL_PERMUTATION_METHODS = ('none', 'decreasing_diagonal_values', 'increasing_**

Supported permutation methods for decompose dense and sparse matrices.

matrix.**SPARSE_ONLY_PERMUTATION_METHODS = ()**

Supported permutation methods only for sparse matrices.

matrix.**DECOMPOSITION_TYPES = ('LDL', 'LDL_compressed', 'LL')**

Supported types of decompositions.

4.1.2 approximate a matrix

matrix.approximate.**decomposition**(*A*, *min_diag_B=None*, *max_diag_B=None*, *min_diag_D=None*, *max_diag_D=None*, *min_abs_value_D=None*, *permutation=None*, *overwrite_A=False*, *return_type=None*)

Computes an approximative decomposition of a matrix with the specified properties.

Returns a decomposition of *A* if has such a decomposition and otherwise a decomposition of an approximation of *A*.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be approximated by a decomposition. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **min_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the composed matrix *B* of an approximated *LDL* decomposition is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the composed matrix *B* of an approximated *LDL* decomposition is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in an approximated *LDL* decomposition is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater or equal to 0. optional, default : 0
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in an approximated *LDL* decomposition is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix *D* of an approximated *LDL* decomposition. optional, default : _matrix-The square root of the resolution of the underlying data type.
- **permutation** (*str or numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.APPROXIMATION_PERMUTATION_METHODS*. If *A* is sparse, it can also be a value in

matrix.SPARSE_ONLY_PERMUTATION_METHODS. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.

- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A. Enabling may result in performance gain. optional, default: False
- **return_type** (*str*) – The type of the decomposition that should be returned. It has to be a value in *matrix.DECOMPOSITION_TYPES*. optional, default : The type of the decomposition is chosen by the function itself.

Returns An (approximative) decomposition of *A* of type *return_type*.

Return type *matrix.decompositions.DecompositionBase*

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixComplexDiagonalValueError* – If *A* has complex diagonal values.

matrix.approximate.**positive_semidefinite_matrix**(*A*, *min_diag_B=None*, *max_diag_B=None*, *min_diag_D=None*, *max_diag_D=None*, *min_abs_value_D=None*, *permutation=None*, *overwrite_A=False*)

Computes a positive semidefinite approximation of *A*.

Returns *A* if *A* is positive semidefinite and otherwise an approximation of *A*.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be approximated. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **min_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a *LDL* decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater or equal to 0. optional, default : 0
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a *LDL* decomposition of the returned matrix is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix *D* in a *LDL* decomposition of the returned matrix. optional, default : _matrixThe square root of the resolution of the underlying data type.
- **permutation** (*str or numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.APPROXIMATION_PERMUTATION_METHODS*. If *A* is sparse, it can also be a value in *matrix.SPARSE_ONLY_PERMUTATION_METHODS*. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.

- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A. Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which has a *LDL* decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix (same type as *A*)

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixComplexDiagonalValueError* – If *A* has complex diagonal values.

matrix.approximate.**positive_definite_matrix**(*A*, *min_diag_B=None*, *max_diag_B=None*, *min_diag_D=None*, *max_diag_D=None*, *min_abs_value_D=None*, *permutation=None*, *overwrite_A=False*)

Computes a positive definite approximation of *A*.

Returns *A* if *A* is positive definite and otherwise an approximation of *A*.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be approximated. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **min_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a *LDL* decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater than 0. optional, default : The square root of the resolution of the underlying data type.
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a *LDL* decomposition of the returned matrix is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix *D* in a *LDL* decomposition of the returned matrix. optional, default : _matrixThe square root of the resolution of the underlying data type.
- **permutation** (*str or numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.APPROXIMATION_PERMUTATION_METHODS*. If *A* is sparse, it can also be a value in *matrix.SPARSE_ONLY_PERMUTATION_METHODS*. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A. Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which has a *LDL* decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix (same type as *A*)

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.

- *matrix.errors.MatrixComplexDiagonalValueError* – If *A* has complex diagonal values.

matrix.**APPROXIMATION_PERMUTATION_METHODS = ('none', 'decreasing_diagonal_values', 'increas**
Supported permutation methods for approximate dense and sparse matrices.

4.1.3 examine a matrix

matrix.**is_invertible**(*A*, *check_finite=True*)
Returns whether the passed matrix is an invertible matrix.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is invertible.

Return type bool

Raises *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.

matrix.**is_positive_semidefinite**(*A*, *check_finite=True*)
Returns whether the passed matrix is positive semi-definite.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive semi-definite.

Return type bool

Raises *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.

matrix.**is_positive_definite**(*A*, *check_finite=True*)
Returns whether the passed matrix is positive definite.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive definite.

Return type bool

Raises *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.

4.1.4 solve system of linear equations

matrix.**solve**(*A*, *b*, *overwrite_b=False*, *check_finite=True*)

Solves the equation $A\ x = b$ regarding x.

Parameters

- **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be checked. It is assumed, that A is Hermitian. The matrix must be a squared matrix.
- **b** (*numpy.ndarray*) – Right-hand side vector or matrix in equation $A\ x = b$. Ii must hold *b.shape[0] == A.shape[0]*.
- **overwrite_b** (*bool*) – Allow overwriting data in *b*. Enabling gives a performance gain. optional, default: False
- **check_finite** (*bool*) – Whether to check that *A* and b‘ contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns An x so that $A\ x = b$. The shape of x matches the shape of b.

Return type numpy.ndarray

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.
- *matrix.errors.MatrixSingularError* – If *A* is singular.

4.2 Matrix decompositions

Several matrix decompositions are supported. They are available in *matrix.decompositions*:

4.2.1 LL decomposition

class matrix.decompositions.**LL_Decomposition**(*L=None*, *p=None*)

Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. This decomposition is also called Cholesky decomposition.

Parameters

- **L** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix L of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of A[p[:, np.newaxis], p[np.newaxis, :]] where A is a matrix. optional, default: no permutation

L

numpy.matrix or scipy.sparse.spmatrix – The matrix L of the decomposition.

P
scipy.sparse.dok_matrix – The permutation matrix. P @ A @ P.T is the matrix A permuted by the permutation of the decomposition

as_LDL_Decomposition()

as_any_type(**type_strs*, *copy=False*)
Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type(*type_str*, *copy=False*)
Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite(*check_finite=True*)
Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible()
Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix
numpy.matrix or scipy.sparse.spmatrix – The composed matrix represented by this decomposition.

copy()
Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

inverse_matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ B @ x*, where *B* is the mattrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*)
Calculates the right side (matrix-matrix or matrix-vector) product *B @ x*, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *B @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *B @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)
Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type bool

is_equal(*other*)
Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type bool

is_finite()
Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type bool

is_invertible()
Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type bool

is_permuted
`bool` – Whether this is a decompositon with permutation.

is_positive_definite()
Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type bool

is_positive_semidefinite()
Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type bool

is_singular()
Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type bool

is_sparse()
Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type bool

is_type(*type_str*)
Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type bool

load(*filename*)
Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

matrix_right_side_multiplication(*x*)
Calculates the right side (matrix-matrix or matrix-vector) product *A* @ *x*, where *A* is the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *A* @ *x*. It must hold *self.n == x.shape[0]*.

Returns The result of *A* @ *x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

n
`int` – The dimension of the squared decomposed matrix.

p
`numpy.ndarray` – The permutation vector. A[p[:, np.newaxis], p[np.newaxis, :]] is the matrix A permuted by the permutation of the decomposition

p_inverse
`numpy.ndarray` – The permutation vector that undos the permutation.

permute_matrix(*A*)
Permute a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

save(*filename*)
Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve(*b*)
Solves the equation *A x = b* regarding *x*, where *A* is the composed matrix represented by this decomposition.

Parameters **b** (*numpy.ndarray or scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation *A x = b*. It must hold *self.n == b.shape[0]*.

Returns An *x* so that *A x = b*. The shape of *x* matches the shape of *b*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'LL'
`str` – The type of this decomposition represented as string.

unpermute_matrix(*A*)
Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

4.2.2 LDL decomposition

class matrix.decompositions.**LDL_Decomposition**(*L=None*, *d=None*, *p=None*)
Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. *D* is a diagonal matrix. Only the diagonal values of *D* are stored.

Parameters

- **L** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix *L* of the decomposition. optional, If it is not set yet, it must be set later.
- **d** (*numpy.ndarray*) – The vector of the diagonal components of *D* of the decompositon. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of A[p[:, np.newaxis], p[np.newaxis, :]] where A is a matrix. optional, default: no permutation

D
scipy.sparse.dia_matrix – The permutation matrix.

L
numpy.matrix or scipy.sparse.spmatrix – The matrix *L* of the decomposition.

LD
numpy.matrix or scipy.sparse.spmatrix – A matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*.

P
scipy.sparse.dok_matrix – The permutation matrix. P @ A @ P.T is the matrix A permuted by the permutation of the decomposition

as_LDL_DecompositionCompressed()

as_LL_Decomposition()

as_any_type(**type_strs*, *copy=False*)
Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type(*type_str*, *copy=False*)
Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.

- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite(*check_finite=True*)
Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible()
Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix
numpy.matrix or scipy.sparse.spmatrix – The composed matrix represented by this decomposition.

copy()
Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

d
numpy.ndarray – The diagonal vector of the matrix D of the decomposition.

inverse_matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product $y.H \ @ \ B \ @ \ x$, where B is the mattrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H \ @ \ B \ @ \ x$. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H \ @ \ B \ @ \ x$. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of $x.H \ @ \ A \ @ \ y$.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*)
Calculates the right side (matrix-matrix or matrix-vector) product $B \ @ \ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B \ @ \ x$. It must hold *self.n == x.shape[0]*.

Returns The result of $B \ @ \ x$.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)
Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type bool

is_equal(*other*)
Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type bool

is_finite()
Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type bool

is_invertible()
Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type bool

is_permuted
bool – Whether this is a decompositon with permutation.

is_positive_definite()
Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type bool

is_positive_semidefinite()
Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type bool

is_singular()
Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type bool

is_sparse()
Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type bool

is_type(*type_str*)
Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type bool

load(*filename*)
Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises FileNotFoundError – If the files are not found in the passed directory.

matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

matrix_right_side_multiplication(*x*)
Calculates the right side (matrix-matrix or matrix-vector) product *A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *A @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *A @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

n
int – The dimension of the squared decomposed matrix.

p
numpy.ndarray – The permutation vector. A[p[:, np.newaxis], p[np.newaxis, :]] is the matrix A permuted by the permutation of the decomposition

p_inverse
numpy.ndarray – The permutation vector that undos the permutation.

permute_matrix(*A*)
Permute a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

save(*filename*)
Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve(*b*)
Solves the equation $A\ x = b$ regarding x, where A is the composed matrix represented by this decomposition.

Parameters **b** (*numpy.ndarray or scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation $A\ x = b$. It must hold *self.n == b.shape[0]*.

Returns An x so that $A\ x = b$. The shape of x matches the shape of b.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'LDL'
str – The type of this decomposition represented as string.

unpermute_matrix(*A*)
Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix A unpermuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

4.2.3 LDL decomposition compressed

class matrix.decompositions.**LDL_DecompositionCompressed**(*LD=None*, *p=None*)
Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. D is a diagonal matrix. L and D are stored in one matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L.

Parameters

- **LD** (*numpy.ndarray or scipy.sparse.spmatrix*) – A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of A[p[:, np.newaxis], p[np.newaxis, :]] where A is a matrix. optional, default: no permutation

D
scipy.sparse.dia_matrix – The permutation matrix.

L
numpy.matrix or scipy.sparse.spmatrix – The matrix L of the decomposition.

LD
numpy.matrix or scipy.sparse.spmatrix – A matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*.

P
scipy.sparse.dok_matrix – The permutation matrix. P @ A @ P.T is the matrix A permuted by the permutation of the decomposition

as_LDL_Decomposition()

as_any_type(**type_strs*, *copy=False*)
Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type(*type_str*, *copy=False*)
Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite(*check_finite=True*)
Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible()
Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix
numpy.matrix or scipy.sparse.spmatrix – The composed matrix represented by this decomposition.

copy()
Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

d

numpy.ndarray – The diagonal vector of the matrix *D* of the decomposition.

inverse_matrix_both_sides_multiplication(*x*, *y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ B @ x*, where *B* is the mattrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*)

Calculates the right side (matrix-matrix or matrix-vector) product *B @ x*, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *B @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *B @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type bool

is_equal(*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type bool

is_finite()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type bool

is_invertible()
Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type bool

is_permuted
bool – Whether this is a decompositon with permutation.

is_positive_definite()
Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type bool

is_positive_semidefinite()
Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type bool

is_singular()
Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type bool

is_sparse()
Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type bool

is_type(*type_str*)
Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type bool

load(*filename*)
Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises FileNotFoundError – If the files are not found in the passed directory.

matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == x.shape[0]*.

- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

matrix_right_side_multiplication(*x*)

Calculates the right side (matrix-matrix or matrix-vector) product *A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *A @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *A @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

n

int – The dimension of the squared decomposed matrix.

p

numpy.ndarray – The permutation vector. A[p[:, np.newaxis], p[np.newaxis, :]] is the matrix A permuted by the permutation of the decomposition

p_inverse

numpy.ndarray – The permutation vector that undos the permutation.

permute_matrix(*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

save(*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve(*b*)

Solves the equation *A x = b* regarding *x*, where *A* is the composed matrix represented by this decomposition.

Parameters **b** (*numpy.ndarray or scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation *A x = b*. It must hold *self.n == b.shape[0]*.

Returns An *x* so that *A x = b*. The shape of *x* matches the shape of *b*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'LDL_compressed'

str – The type of this decomposition represented as string.

unpermute_matrix(*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

4.2.4 base decomposition

class matrix.decompositions.**DecompositionBase**(*p=None*)

Bases: object

A matrix decomposition.

This class is a base class for matrix decompositions.

Parameters **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of A[p[:, np.newaxis], p[np.newaxis, :]] where A is a matrix. optional, default: no permutation

P

scipy.sparse.dok_matrix – The permutation matrix. P @ A @ P.T is the matrix A permuted by the permutation of the decomposition

as_any_type(**type_strs*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type(*type_str*, *copy=False*)

Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite(*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible()
Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix
numpy.matrix or scipy.sparse.spmatrix – The composed matrix represented by this decomposition.

copy()
Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

inverse_matrix_both_sides_multiplication(*x*, *y=None*)
Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ B @ x*, where *B* is the mattrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ B @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*)
Calculates the right side (matrix-matrix or matrix-vector) product *B @ x*, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *B @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *B @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)
Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type bool

is_equal(*other*)
Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type bool

is_finite()
Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type bool

is_invertible()
Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type bool

is_permuted
bool – Whether this is a decompositon with permutation.

is_positive_definite()
Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type bool

is_positive_semidefinite()
Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type bool

is_singular()
Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type bool

is_sparse()
Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type bool

is_type(*type_str*)
Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type bool

load(*filename*)
Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication(*x*, *y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product *y.H @ A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == x.shape[0]*.
- **y** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product *y.H @ A @ x*. It must hold *self.n == y.shape[0]*. optional, default: If y is not passed, x is used as y.

Returns The result of *x.H @ A @ y*.

Return type numpy.ndarray or scipy.sparse.spmatrix

matrix_right_side_multiplication(*x*)

Calculates the right side (matrix-matrix or matrix-vector) product *A @ x*, where *A* is the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray or scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector *A @ x*. It must hold *self.n == x.shape[0]*.

Returns The result of *A @ x*.

Return type numpy.ndarray or scipy.sparse.spmatrix

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. A[p[:, np.newaxis], p[np.newaxis, :]] is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undos the permutation.

permute_matrix(*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

save(*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve(*b*)

Solves the equation *A x = b* regarding *x*, where *A* is the composed matrix represented by this decomposition.

Parameters **b** (*numpy.ndarray or scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation *A x = b*. It must hold *self.n == b.shape[0]*.

Returns An *x* so that *A x = b*. The shape of *x* matches the shape of *b*.

Return type numpy.ndarray or scipy.sparse.spmatrix

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'base'
str – The type of this decomposition represented as string.

unpermute_matrix(*A*)
Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray or scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type numpy.ndarray or scipy.sparse.spmatrix

4.3 Errors

This is an overview about the exceptions that could arise in this package. They are available in *matrix.errors*:

If a matrix should be decomposed with *matrix.decompose* and the desired decomposition is not computable, the following exceptions can be raised:

4.3.1 NoDecompositionPossibleError

class matrix.errors.**NoDecompositionPossibleError**(*base*, *desired_type*)
Bases: *matrix.errors.BaseError*

It is to possible to calculate a desired matrix decomposition.

4.3.2 NoDecompositionPossibleWithProblematicSubdecompositionError

class matrix.errors.**NoDecompositionPossibleWithProblematicSubdecompositionError**(*base*, *desired_type*, *problematic_leading_pr* *subdecomposition=None*)
Bases: *matrix.errors.NoDecompositionPossibleError*

It is not possible to calculate a desired matrix decomposition. Only a subdecompostion could be calculated

4.3.3 NoDecompositionPossibleTooManyEntriesError

class matrix.errors.**NoDecompositionPossibleTooManyEntriesError**(*matrix*, *desired_type*)
Bases: *matrix.errors.NoDecompositionPossibleError*

The matrix decomposition is not possible for this matrix because it would have too many entries.

4.3.4 NoDecompositionConversionImplementedError

class matrix.errors.**NoDecompositionConversionImplementedError**(*decomposition*, *desired_type*)

Bases: *matrix.errors.NoDecompositionPossibleError*

A decomposition conversion is not implemented for this type.

If a matrix has an invalid characteristic, the following exceptions can occur:

4.3.5 MatrixNotSquareError

class matrix.errors.**MatrixNotSquareError**(*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix is not a square matrix although this is required.

4.3.6 MatrixNotFiniteError

class matrix.errors.**MatrixNotFiniteError**(*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix has non-finite entries although a finite matrix is required.

4.3.7 MatrixSingularError

class matrix.errors.**MatrixSingularError**(*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix is singular although an invertible matrix is required.

4.3.8 MatrixNotHermitianError

class matrix.errors.**MatrixNotHermitianError**(*matrix*, *i=None*, *j=None*)

Bases: *matrix.errors.MatrixError*

A matrix is not Hermitian although a Hermitian matrix is required.

4.3.9 MatrixComplexDiagonalValueError

class matrix.errors.**MatrixComplexDiagonalValueError**(*matrix*, *i=None*)

Bases: *matrix.errors.MatrixNotHermitianError*

A matrix has complex diagonal values although real diagonal values are required.

All these exceptions are based on the following exception:

4.3.10 MatrixError

class matrix.errors.**MatrixError**(*matrix*, *message=None*)

Bases: *matrix.errors.BaseError*

An exception related to a matrix.

If the matrix represented by a decomposition has an invalid characteristic, the following exceptions can occur:

4.3.11 DecompositionNotFiniteError

class matrix.errors.**DecompositionNotFiniteError**(*decomposition*)
Bases: *matrix.errors.DecompositionError*

A decomposition of a matrix has non-finite entries although a finite matrix is required.

4.3.12 DecompositionSingularError

class matrix.errors.**DecompositionSingularError**(*decomposition*)
Bases: *matrix.errors.DecompositionError*

A decomposition represents a singular matrix although a non-singular matrix is required.

If a decomposition should be loaded from a file which is not a valid decomposition file, the following exception is raised:

4.3.13 DecompositionInvalidFile

class matrix.errors.**DecompositionInvalidFile**(*filename*)
Bases: *matrix.errors.DecompositionError*, OSError

A decomposition indicated that a decomposition should be loaded from an invalid file.

If a decomposition should be loaded from a file which caontains a type which does not fit to the type of the decomposition where it should be loaded into, the following exception is raised:

4.3.14 DecompositionInvalidDecompositionTypeFile

class matrix.errors.**DecompositionInvalidDecompositionTypeFile**(*filename*, *type_file*, *type_needed*)
Bases: *matrix.errors.DecompositionInvalidFile*

A decomposition indicated that a decomposition should be loaded from an file in which another decomposition type is stored.

All these exceptions are based on the following exception:

4.3.15 DecompositionError

class matrix.errors.**DecompositionError**(*decomposition*, *message=None*)
Bases: *matrix.errors.BaseError*

An exception related to a decomposition.

The following exception is the base exception from which all other exceptions in this package are derived:

4.3.16 BaseError

class matrix.errors.**BaseError**(*message*)
Bases: Exception

This is the base exception for all exceptions in this package.

4.4 Changelog

4.4.1 0.8

- Approximation functions are replaced by more sophisticated approximation functions.
- Explicit function for approximating a matrix by a positive (semi)definite matrix is added.
- Universal save and load functions are added.
- Decompositions obtain is_equal and is_almost_equal methods.
- Functions to multiply the matrix represented by a decomposition or its inverse with a matrix or a vector are added.
- Allow to directly pass a permutation vector to approximate and decompose methods.

4.4.2 0.7

- Lineare systems associated to matrices or decompositions can now be solved.
- Invertibility of matrices and decompositions can now be examined.
- Decompositions can now be examined to see if they contain only finite values.

4.4.3 0.6

- Decompositions are now saveable and loadable.

4.4.4 0.5

- Matrices can now be approximated by decompositions.

4.4.5 0.4

- Positive definiteness and positive semi-definiteness of matrices and decompositions can now be examined.

4.4.6 0.3

- Dense and sparse matrices are now decomposable into several types (LL, LDL, LDL compressed).

4.4.7 0.2

- Decompositons are now convertable to other decompositon types.
- Decompositions are now comparable.

4.4.8 0.1

- Several decompositions types are added (LL, LDL, LDL compressed).
- Several permutation capabilities added.

CHAPTER 5

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