
matrix_decomposition Documentation

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This is *matrix-decomposition*, a library to approximate Hermitian (dense and sparse) matrices by positive definite matrices. Furthermore it allows to decompose (factorize) positive definite matrices and solve associated systems of linear equations.

There are several ways to obtain and install this package.

1.1 Conda

To install this package with *conda* run:

```
conda install -c jore matrix-decomposition
```

<https://anaconda.org/jore/matrix-decomposition>

1.2 pip

To install this package with *pip* run:

```
pip install 'matrix-decomposition'
```

<https://pypi.python.org/pypi/matrix-decomposition>

1.3 GitHub

To clone this package with *git* run:

```
git clone https://github.com/jor-/matrix-decomposition.git
```

To install this package after that with *python* run:

```
cd matrix-decomposition; python setup.py install
```

<https://github.com/jor-/matrix-decomposition>

CHAPTER 2

Documentation

<https://matrix-decomposition.readthedocs.io>

CHAPTER 3

Test status

4.1 Functions

Several functions are included in this package. The most important ones are summarized here.

4.1.1 Decompose a matrix

`matrix.decompose` (*A*, *permutation=None*, *return_type=None*, *check_finite=True*, *overwrite_A=False*)

Computes a decomposition of a matrix.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Matrix to be decomposed. *A* must be Hermitian.
- **permutation** (*str* or *numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in `matrix.UNIVERSAL_PERMUTATION_METHODS`. If *A* is sparse, it can also be a value in `matrix.SPARSE_ONLY_PERMUTATION_METHODS`. It is also possible to directly pass a permutation vector. optional, default: no permutation
- **return_type** (*str*) – The type of the decomposition that should be calculated. It has to be a value in `matrix.DECOMPOSITION_TYPES`. If *return_type* is `None` the type of the returned decomposition is chosen by the function itself. optional, default: the type of the decomposition is chosen by the function itself
- **check_finite** (*bool*) – Whether to check that *A* contains only finite numbers. Disabling may result in problems (crashes, non-termination) if the inputs do contain infinities or NaNs. Disabling gives a performance gain. optional, default: `True`
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: `False`

Returns A decomposition of *A* of type *return_type*.

Return type *matrix.decompositions.DecompositionBase*

Raises

- *matrix.errors.NoDecompositionPossibleError* – If the decomposition of A is not possible.
- *matrix.errors.MatrixNotSquareError* – If A is not a square matrix.
- *matrix.errors.MatrixNotFiniteError* – If A is not a finite matrix and *check_finite* is True.

`matrix.UNIVERSAL_PERMUTATION_METHODS = ('none', 'decreasing_diagonal_values', 'increasing_`
Supported permutation methods for decompose dense and sparse matrices.

`matrix.SPARSE_ONLY_PERMUTATION_METHODS = ()`
Supported permutation methods only for sparse matrices.

`matrix.DECOMPOSITION_TYPES = ('LDL', 'LDL_compressed', 'LL')`
Supported types of decompositions.

4.1.2 Approximate a matrix

`matrix.approximate.decomposition(A, min_diag_B=None, max_diag_B=None,`
`min_diag_D=None, max_diag_D=None,`
`min_abs_value_D=None, permutation=None, over-`
`write_A=False, return_type=None)`

Computes an approximative decomposition of a matrix with the specified properties.

Returns a decomposition of A if has such a decomposition and otherwise a decomposition of an approximation of A .

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be approximated by a decomposition. A must be Hermitian.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the composed matrix B of an approximated LDL^H decomposition is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the composed matrix B of an approximated LDL^H decomposition is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix D in an approximated LDL^H decomposition is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater than 0. optional, default : The square root of the resolution of the underlying data type.
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix D in an approximated LDL^H decomposition is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix D of an approximated LDL^H decomposition. *min_abs_value_D* must be greater or equal to 0. optional, default : The square root of the resolution of the underlying data type.
- **permutation** (*str* or *numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be

a value in `matrix.UNIVERSAL_PERMUTATION_METHODS` or `matrix.APPROXIMATION_ONLY_PERMUTATION_METHODS`. If A is sparse, it can also be a value in `matrix.SPARSE_ONLY_PERMUTATION_METHODS`. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.

- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A . Enabling may result in performance gain. optional, default: False
- **return_type** (*str*) – The type of the decomposition that should be returned. It has to be a value in `matrix.DECOMPOSITION_TYPES`. optional, default : The type of the decomposition is chosen by the function itself.

Returns An (approximative) decomposition of A of type *return_type*.

Return type `matrix.decompositions.DecompositionBase`

Raises

- `matrix.errors.MatrixNotSquareError` – If A is not a square matrix.
- `matrix.errors.MatrixComplexDiagonalValueError` – If A has complex diagonal values.

`matrix.approximate.positive_definite_matrix` (A , *min_diag_B=None*, *max_diag_B=None*,
min_diag_D=None, *max_diag_D=None*,
permutation=None, *overwrite_A=False*)

Computes a positive definite approximation of A .

Returns A if A is positive definite and otherwise an approximation of A .

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be approximated. A must be Hermitian.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix D in a LDL^H decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater than 0. optional, default : The square root of the resolution of the underlying data type.
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix D in a LDL^H decomposition of the returned matrix is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **permutation** (*str* or *numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in `matrix.UNIVERSAL_PERMUTATION_METHODS` or `matrix.APPROXIMATION_ONLY_PERMUTATION_METHODS`. If A is sparse, it can also be a value in `matrix.SPARSE_ONLY_PERMUTATION_METHODS`. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A . Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which is positive definite.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix` (same type as *A*)

Raises

- `matrix.errors.MatrixNotSquareError` – If *A* is not a square matrix.
- `matrix.errors.MatrixComplexDiagonalValueError` – If *A* has complex diagonal values.

`matrix.APPROXIMATION_ONLY_PERMUTATION_METHODS = ('minimal_difference',)`
Supported permutation methods only for approximate dense and sparse matrices.

4.1.3 Examine a matrix

`matrix.is_positive_semidefinite(A, check_finite=True)`

Returns whether the passed matrix is positive semi-definite.

Parameters

- **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be checked. *A* must be Hermitian.
- **check_finite** (`bool`) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive semi-definite.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If *A* is not a finite matrix and `check_finite` is True.

`matrix.is_positive_definite(A, check_finite=True)`

Returns whether the passed matrix is positive definite.

Parameters

- **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be checked. *A* must be Hermitian.
- **check_finite** (`bool`) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive definite.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If *A* is not a finite matrix and `check_finite` is True.

`matrix.is_invertible(A, check_finite=True)`

Returns whether the passed matrix is an invertible matrix.

Parameters

- **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be checked. *A* must be Hermitian and positive semidefinite.

- **check_finite** (*bool*) – Whether to check that A contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether A is invertible.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If A is not a finite matrix and `check_finite` is True.

4.1.4 Solve system of linear equations

`matrix.solve(A, b, overwrite_b=False, check_finite=True)`

Solves the equation $Ax = b$ regarding x .

Parameters

- **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be checked. A must be Hermitian and positive definite.
- **b** (`numpy.ndarray`) – Right-hand side vector or matrix in equation $Ax = b$. It must hold `b.shape[0] == A.shape[0]`.
- **overwrite_b** (*bool*) – Allow overwriting data in b . Enabling gives a performance gain. optional, default: False
- **check_finite** (*bool*) – Whether to check that A and b^* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns An x so that $Ax = b$. The shape of x matches the shape of b .

Return type `numpy.ndarray`

Raises

- `matrix.errors.MatrixNotSquareError` – If A is not a square matrix.
- `matrix.errors.MatrixNotFiniteError` – If A is not a finite matrix and `check_finite` is True.
- `matrix.errors.MatrixSingularError` – If A is singular.

4.2 Matrix decompositions

Several matrix decompositions are supported. They are available in `matrix.decompositions`:

4.2.1 LL decomposition

class `matrix.decompositions.LL_Decomposition` ($L=None, p=None$)

Bases: `matrix.decompositions.DecompositionBase`

A matrix decomposition where LL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. This decomposition is also called Cholesky decomposition.

Parameters

- **L** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix L of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

L

numpy.matrix or *scipy.sparse.spmatrix* – The matrix L of the decomposition.

P

scipy.sparse.dok_matrix – The permutation matrix. $P @ A @ P.T$ is the matrix A permuted by the permutation of the decomposition

as_LDL_Decomposition()

as_any_type (**type_strs*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type (*type_str*, *copy=False*)

Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

inverse_matrix_both_sides_multiplication(*x*, *y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == y.shape[0]`. optional, default: If *y* is not passed, *x* is used as *y*.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (`str`) – The decomposition which to compare to this decomposition.
- **rtol** (`float`) – The relative tolerance parameter.
- **atol** (`float`) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal(*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (`str`) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

`bool` – Whether this is a decompositon with permutation.

is_positive_definite()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type(type_str)

Whether this is a decomposition of the passed type.

Parameters `type_str (str)` – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(filename)

Loads a decomposition of this type.

Parameters `filename (str)` – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication(x, y=None)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == y.shape[0]`. optional, default: If y is not passed, x is used as y.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix (*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*filename*)

Saves this decomposition.

Parameters **filename** (`str`) – Where this decomposition should be saved.

solve (*b*)

Solves the equation $A x = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters **b** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Right-hand side vector or matrix in equation $A x = b$. It must hold `self.n == b.shape[0]`.

Returns An x so that $A x = b$. The shape of x matches the shape of b .

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

type_str = 'LL'

`str` – The type of this decomposition represented as string.

unpermute_matrix (*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

4.2.2 LDL decomposition

class `matrix.decompositions.LDL_Decomposition` (*L=None, d=None, p=None*)

Bases: `matrix.decompositions.DecompositionBase`

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. *D* is a diagonal matrix. Only the diagonal values of *D* are stored.

Parameters

- **L** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix *L* of the decomposition. optional, If it is not set yet, it must be set later.
- **d** (*numpy.ndarray*) – The vector of the diagonal components of *D* of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where *A* is a matrix. optional, default: no permutation

D

scipy.sparse.dia_matrix – The permutation matrix.

L

numpy.matrix or *scipy.sparse.spmatrix* – The matrix *L* of the decomposition.

LD

numpy.matrix or *scipy.sparse.spmatrix* – A matrix whose diagonal values are the diagonal values of *D* and whose off-diagonal values are those of *L*.

P

scipy.sparse.dok_matrix – The permutation matrix. $P @ A @ P.T$ is the matrix *A* permuted by the permutation of the decomposition

as_LDL_DecompositionCompressed ()

as_LL_Decomposition ()

as_any_type (**type_strs*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in `type_strs`, a decomposition of type `type_str[0]` is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on `copy`.

Return type `matrix.decompositions.DecompositionBase`

as_type (`type_str`, `copy=False`)

Convert decomposition to passed type.

Parameters

- **type_str** (`str`) – The decomposition type to which this decomposition is converted.
- **copy** (`bool`) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not `type_str`, a decomposition of type `type_str` is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on `copy`.

Return type `matrix.decompositions.DecompositionBase`

check_finite (`check_finite=True`)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (`bool`) – Whether to perform this check. default: True

Raises `matrix.errors.DecompositionNotFiniteError` – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy ()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

d

`numpy.ndarray` – The diagonal vector of the matrix D of the decomposition.

inverse_matrix_both_sides_multiplication (`x`, `y=None`)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == y.shape[0]`. optional, default: If y is not passed, x is used as y.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

`inverse_matrix_right_side_multiplication(x)`

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **`x`** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

`is_almost_equal(other, rtol=0.0001, atol=1e-06)`

Whether this decomposition is close to passed decomposition.

Parameters

- **`other`** (`str`) – The decomposition which to compare to this decomposition.
- **`rtol`** (`float`) – The relative tolerance parameter.
- **`atol`** (`float`) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

`is_equal(other)`

Whether this decomposition is equal to passed decomposition.

Parameters **`other`** (`str`) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

`is_finite()`

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

`is_invertible()`

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

`is_permuted`

`bool` – Whether this is a decompositon with permutation.

`is_positive_definite()`

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type(type_str)

Whether this is a decomposition of the passed type.

Parameters `type_str (str)` – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(filename)

Loads a decomposition of this type.

Parameters `filename (str)` – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication(x, y=None)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == y.shape[0]`. optional, default: If y is not passed, x is used as y.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication(x)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n

`int` – The dimension of the squared decomposed matrix.

p
`numpy.ndarray` – The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse
`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix(A)
Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save(*filename*)
Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve(b)
Solves the equation $Ax = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters **b** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Right-hand side vector or matrix in equation $Ax = b$. It must hold `self.n == b.shape[0]`.

Returns An x so that $Ax = b$. The shape of x matches the shape of b .

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

type_str = 'LDL'
str – The type of this decomposition represented as string.

unpermute_matrix(A)
Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be unpermuted.

Returns The matrix A unpermuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

4.2.3 LDL decomposition compressed

class `matrix.decompositions.LDL_DecompositionCompressed`($LD=None, p=None$)

Bases: `matrix.decompositions.DecompositionBase`

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. D is a diagonal matrix. L and D are stored in one matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

Parameters

- **LD** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L . optional, If it is not set yet, it must be set later.

- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

D

`scipy.sparse.dia_matrix` – The permutation matrix.

L

`numpy.matrix` or `scipy.sparse.spmatrix` – The matrix L of the decomposition.

LD

`numpy.matrix` or `scipy.sparse.spmatrix` – A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

P

`scipy.sparse.dok_matrix` – The permutation matrix. $P @ A @ P.T$ is the matrix A permuted by the permutation of the decomposition

as_LDL_Decomposition()

as_any_type (**type_strs*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str*[0] is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type (*type_str*, *copy=False*)

Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

composed_matrix

`numpy.matrix` or `scipy.sparse.spmatrix` – The composed matrix represented by this decomposition.

copy()

Copy this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

d

`numpy.ndarray` – The diagonal vector of the matrix D of the decomposition.

inverse_matrix_both_sides_multiplication (x , $y=None$)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == y.shape[0]`. optional, default: If y is not passed, x is used as y .

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication (x)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

is_almost_equal ($other$, $rtol=0.0001$, $atol=1e-06$)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (`str`) – The decomposition which to compare to this decomposition.
- **rtol** (`float`) – The relative tolerance parameter.
- **atol** (`float`) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

`bool` – Whether this is a decompositon with permutation.

is_positive_definite ()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite ()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular ()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse ()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type (*type_str*)

Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load (*filename*)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication (*x*, *y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == y.shape[0]`. optional, default: If *y* is not passed, *x* is used as *y*.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix (*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*filename*)

Saves this decomposition.

Parameters **filename** (`str`) – Where this decomposition should be saved.

solve (*b*)

Solves the equation $A x = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters **b** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Right-hand side vector or matrix in equation $A x = b$. It must hold `self.n == b.shape[0]`.

Returns An x so that $A x = b$. The shape of x matches the shape of b .

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

type_str = 'LDL_compressed'

str – The type of this decomposition represented as string.

unpermute_matrix(*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters *A* (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

4.2.4 Base decomposition

class `matrix.decompositions.DecompositionBase` (*p=None*)

Bases: `object`

A matrix decomposition.

This class is a base class for all other matrix decompositions.

Parameters *p* (`numpy.ndarray`) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where *A* is a matrix. optional, default: no permutation

P

`scipy.sparse.dok_matrix` – The permutation matrix. $P @ A @ P.T$ is the matrix *A* permuted by the permutation of the decomposition

as_any_type (**type_strs*, *copy=False*)

Convert decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

as_type (*type_str*, *copy=False*)

Convert decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix

numpy.matrix or *scipy.sparse.spmatrix* – The composed matrix represented by this decomposition.

copy ()

Copy this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

inverse_matrix_both_sides_multiplication (*x, y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == x.shape[0]$.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.

Returns The result of $x.H @ A @ y$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication (*x*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold $self.n == x.shape[0]$.

Returns The result of $B @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal (*other, rtol=0.0001, atol=1e-06*)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

`bool` – Whether this is a decompositon with permutation.

is_positive_definite ()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite ()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular ()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse ()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type (*type_str*)

Whether this is a decomposition of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load (*filename*)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises `FileNotFoundError` – If the files are not found in the passed directory.

matrix_both_sides_multiplication (*x*, *y=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == y.shape[0]`. optional, default: If *y* is not passed, *x* is used as *y*.

Returns The result of $x.H @ A @ y$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold `self.n == x.shape[0]`.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n

`int` – The dimension of the squared decomposed matrix.

p

`numpy.ndarray` – The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

p_inverse

`numpy.ndarray` – The permutation vector that undoes the permutation.

permute_matrix (*A*)

Permute a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve (*b*)

Solves the equation $A x = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters **b** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation $A x = b$. It must hold *self.n* == *b.shape[0]*.

Returns An x so that $A x = b$. The shape of x matches the shape of b .

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'base'

str – The type of this decomposition represented as string.

unpermute_matrix (*A*)

Unpermute a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix A unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

4.3 Errors

This is an overview about the exceptions that could arise in this package. They are available in *matrix.errors*:

If a matrix should be decomposed with *matrix.decompose* and the desired decomposition is not computable, the following exceptions can be raised:

4.3.1 NoDecompositionPossibleError

class *matrix.errors.NoDecompositionPossibleError* (*base, desired_type*)

Bases: *matrix.errors.BaseError*

It is not possible to calculate a desired matrix decomposition.

4.3.2 NoDecompositionPossibleWithProblematicSubdecompositionError

class *matrix.errors.NoDecompositionPossibleWithProblematicSubdecompositionError* (*base, desired_type, problematic_leading_principal_subdecomposition=None*)

Bases: *matrix.errors.NoDecompositionPossibleError*

It is not possible to calculate a desired matrix decomposition. Only a subdecomposition could be calculated

4.3.3 NoDecompositionPossibleTooManyEntriesError

```
class matrix.errors.NoDecompositionPossibleTooManyEntriesError (matrix,      de-
                                                                sired_type)
```

Bases: *matrix.errors.NoDecompositionPossibleError*

The decomposition is not possible for this matrix because it would have too many entries.

4.3.4 NoDecompositionConversionImplementedError

```
class matrix.errors.NoDecompositionConversionImplementedError (decomposition,
                                                                desired_type)
```

Bases: *matrix.errors.NoDecompositionPossibleError*

A decomposition conversion is not implemented for this type.

If a matrix has an invalid characteristic, the following exceptions can occur:

4.3.5 MatrixError

```
class matrix.errors.MatrixError (matrix, message=None)
```

Bases: *matrix.errors.BaseError*

An exception related to a matrix.

4.3.6 MatrixNotSquareError

```
class matrix.errors.MatrixNotSquareError (matrix)
```

Bases: *matrix.errors.MatrixError*

A matrix is not a square matrix although a square matrix is required.

4.3.7 MatrixNotFiniteError

```
class matrix.errors.MatrixNotFiniteError (matrix)
```

Bases: *matrix.errors.MatrixError*

A matrix has non-finite entries although a finite matrix is required.

4.3.8 MatrixSingularError

```
class matrix.errors.MatrixSingularError (matrix)
```

Bases: *matrix.errors.MatrixError*

A matrix is singular although an invertible matrix is required.

4.3.9 MatrixNotHermitianError

class `matrix.errors.MatrixNotHermitianError` (*matrix, i=None, j=None*)
Bases: `matrix.errors.MatrixError`

A matrix is not Hermitian although a Hermitian matrix is required.

4.3.10 MatrixComplexDiagonalValueError

class `matrix.errors.MatrixComplexDiagonalValueError` (*matrix, i=None*)
Bases: `matrix.errors.MatrixNotHermitianError`

A matrix has complex diagonal values although real diagonal values are required.

If the matrix represented by a decomposition has an invalid characteristic, the following exceptions can occur:

4.3.11 DecompositionError

class `matrix.errors.DecompositionError` (*decomposition, message=None*)
Bases: `matrix.errors.BaseError`

An exception related to a decomposition.

4.3.12 DecompositionNotFiniteError

class `matrix.errors.DecompositionNotFiniteError` (*decomposition*)
Bases: `matrix.errors.DecompositionError`

A decomposition of a matrix has non-finite entries although a finite matrix is required.

4.3.13 DecompositionSingularError

class `matrix.errors.DecompositionSingularError` (*decomposition*)
Bases: `matrix.errors.DecompositionError`

A decomposition represents a singular matrix although a non-singular matrix is required.

If a decomposition should be loaded from a file which is not a valid decomposition file, the following exception is raised:

4.3.14 DecompositionInvalidFile

class `matrix.errors.DecompositionInvalidFile` (*filename*)
Bases: `matrix.errors.DecompositionError, OSError`

An attempt was made to load a decomposition from an invalid file.

If a decomposition should be loaded from a file which contains a type which does not fit to the type of the decomposition where it should be loaded into, the following exception is raised:

4.3.15 DecompositionInvalidDecompositionTypeFile

```
class matrix.errors.DecompositionInvalidDecompositionTypeFile (filename,  
                                                                type_file,  
                                                                type_needed)
```

Bases: `matrix.errors.DecompositionInvalidFile`

An attempt was made to load a decomposition from an file in which another decomposition type is stored.

The following exception is the base exception from which all other exceptions in this package are derived:

4.3.16 BaseError

```
class matrix.errors.BaseError (message)  
    Bases: Exception
```

This is the base exception for all exceptions in this package.

4.4 Changelog

4.4.1 1.0

- Approximation functions are slightly faster now.
- Better overflow handling in approximation functions.
- Prebuild html documentation included.
- Function for approximating a matrix by a positive semidefinite matrix (`matrix.approximate.positive_semidefinite_matrix`) removed.

4.4.2 0.8

- Approximation functions are replaced by more sophisticated approximation functions.
- Explicit function for approximating a matrix by a positive (semi)definite matrix is added.
- Universal save and load functions are added.
- Decompositions obtain `is_equal` and `is_almost_equal` methods.
- Functions to multiply the matrix represented by a decomposition or its inverse with a matrix or a vector are added.
- Allow to directly pass a permutation vector to approximate and decompose methods.

4.4.3 0.7

- Lineare systems associated to matrices or decompositions can now be solved.
- Invertibility of matrices and decompositions can now be examined.
- Decompositions can now be examined to see if they contain only finite values.

4.4.4 0.6

- Decompositions are now saveable and loadable.

4.4.5 0.5

- Matrices can now be approximated by decompositions.

4.4.6 0.4

- Positive definiteness and positive semi-definiteness of matrices and decompositions can now be examined.

4.4.7 0.3

- Dense and sparse matrices are now decomposable into several types (LL, LDL, LDL compressed).

4.4.8 0.2

- Decompositons are now convertible to other decompositon types.
- Decompositions are now comparable.

4.4.9 0.1

- Several decompositions types are added (LL, LDL, LDL compressed).
- Several permutation capabilities added.

CHAPTER 5

Indices and tables

- `genindex`
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CHAPTER 6

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