
matrix_decomposition Documentation

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This is *matrix-decomposition*, a library to approximate Hermitian (dense and sparse) matrices by positive definite matrices. Furthermore it allows to decompose (factorize) positive definite matrices and solve associated systems of linear equations.

There are several ways to obtain and install this package.

1.1 Conda

To install this package with *conda* run:

```
conda install -c jore matrix-decomposition
```

<https://anaconda.org/jore/matrix-decomposition>

1.2 pip

To install this package with *pip* run:

```
pip install 'matrix-decomposition'
```

<https://pypi.python.org/pypi/matrix-decomposition>

1.3 GitHub

To clone this package with *git* run:

```
git clone https://github.com/jor-/matrix-decomposition.git
```

To install this package after that with *python* run:

```
cd matrix-decomposition; python setup.py install
```

<https://github.com/jor-/matrix-decomposition>

1.4 Zenodo

CHAPTER 2

Documentation

<https://matrix-decomposition.readthedocs.io>

CHAPTER 3

Test status

4.1 Functions

Several functions are included in this package. The most important ones are summarized here.

4.1.1 Positive semidefinite approximation of a matrix

`matrix.approximation.positive_semidefinite.positive_semidefinite_matrix` (*A*,
min_diag_B=None,
max_diag_B=None,
min_diag_D=None,
max_diag_D=None,
min_abs_value_D=None,
min_abs_value_L=None,
per-
mu-
ta-
tion=None,
over-
write_A=False)

Computes an approximation of A which has a LDL^H decomposition with the specified properties.

Returns A if A has such a decomposition and otherwise an approximation of A .

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be approximated. A must be Hermitian.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.

- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^H decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater or equal to 0. optional, default : Is chosen by the algorithm.
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^H decomposition of the returned matrix is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix *D* in a LDL^H decomposition of the returned matrix. *min_abs_value_D* must be greater or equal to 0. optional, default : The square root of the resolution of the underlying data type.
- **min_abs_value_L** (*float*) – Absolute values below *min_abs_value_L* are considered as zero in the matrix *L* of an approximated LDL^H decomposition. *min_abs_value_L* must be greater or equal to 0. optional, default : The resolution of the underlying data type.
- **permutation** (*str* or *numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.UNIVERSAL_PERMUTATION_METHODS* or *APPROXIMATION_ONLY_PERMUTATION_METHODS*. If *A* is sparse, it can also be a value in *matrix.SPARSE_ONLY_PERMUTATION_METHODS*. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which has a LDL^H decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix* (same type as *A*)

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixComplexDiagonalValueError* – If *A* has complex diagonal values.

```
matrix.approximation.positive_semidefinite.decomposition(A, min_diag_B=None,
                                                         max_diag_B=None,
                                                         min_diag_D=None,
                                                         max_diag_D=None,
                                                         min_abs_value_D=None,
                                                         min_abs_value_L=None,
                                                         permutation=None,
                                                         overwrite_A=False,
                                                         return_type=None)
```

Computes an approximative decomposition of a matrix with the specified properties.

Returns a decomposition of *A* if has such a decomposition and otherwise a decomposition of an approximation of *A*.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be approximated by a decomposition. *A* must be Hermitian.

- **min_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the composed matrix B of an approximated LDL^H decomposition is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the composed matrix B of an approximated LDL^H decomposition is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix D in an approximated LDL^H decomposition is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be greater or equal to 0. optional, default : Is chosen by the algorithm.
- **max_diag_D** (*float*) – Each component of the diagonal of the matrix D in an approximated LDL^H decomposition is forced to be lower or equal to *max_diag_D*. optional, default : No maximal value is forced.
- **min_abs_value_D** (*float*) – Absolute values below *min_abs_value_D* are considered as zero in the matrix D of an approximated LDL^H decomposition. *min_abs_value_D* must be greater or equal to 0. optional, default : The square root of the resolution of the underlying data type.
- **min_abs_value_L** (*float*) – Absolute values below *min_abs_value_L* are considered as zero in the matrix L of an approximated LDL^H decomposition. *min_abs_value_L* must be greater or equal to 0. optional, default : The resolution of the underlying data type.
- **permutation** (*str or numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in `matrix.UNIVERSAL_PERMUTATION_METHODS` or `APPROXIMATION_ONLY_PERMUTATION_METHODS`. If A is sparse, it can also be a value in `matrix.SPARSE_ONLY_PERMUTATION_METHODS`. It is also possible to directly pass a permutation vector. optional, default: The permutation is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A . Enabling may result in performance gain. optional, default: False
- **return_type** (*str*) – The type of the decomposition that should be returned. It has to be a value in `matrix.DECOMPOSITION_TYPES`. optional, default : The type of the decomposition is chosen by the function itself.

Returns An (approximative) decomposition of A of type *return_type*.

Return type `matrix.decompositions.DecompositionBase`

Raises

- `matrix.errors.MatrixNotSquareError` – If A is not a square matrix.
- `matrix.errors.MatrixComplexDiagonalValueError` – If A has complex diagonal values.

```
matrix.approximation.positive_semidefinite.APPROXIMATION_ONLY_PERMUTATION_METHODS = ('minim
Permutation methods supported only by the decomposition and the positive_semidefinite_matrix algorithm.
```

```
matrix.approximation.positive_semidefinite.GMW_81(A, min_diag_B=None,
max_diag_B=None,
min_diag_D=None, overwrite_A=False)
```

Computes a positive definite approximation of A .

Returns A if A is positive definite and meets the constraints and otherwise a positive definite approximation of A .

Parameters

- **A** (*numpy.ndarray*) – The matrix that should be approximated. *A* must be symmetric.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which is positive definite.

Return type *numpy.ndarray*

Raises *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.

Notes

The algorithm is introduced in [1]. Is is also described in [2]. This discription has been used for this implementation. The implementation has been extended to allow restrictions on the diagonal values.

References

[1] Gill, P. E.; Murray, W. & Wright, M. H., Practical optimization, Academic press, 1981

[2] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349

```
matrix.approximation.positive_semidefinite.GMW_T1 (A, min_diag_B=None,
                                                    max_diag_B=None,
                                                    min_diag_D=None,      over-
                                                    write_A=False)
```

Computes a positive definite approximation of *A*.

Returns *A* if *A* is positive definite and meets the constrains and otherwise a positive definite approximation of *A*.

Parameters

- **A** (*numpy.ndarray*) – The matrix that should be approximated. *A* must be symmetric.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.

- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns *B* – An approximation of *A* which is positive definite.

Return type `numpy.ndarray`

Raises `matrix.errors.MatrixNotSquareError` – If *A* is not a square matrix.

Notes

The algorithm is introduced in [1]. This discription has been used for this implementation. The algorithm is based on [2]. The implementation has been extended to allow restrictions on the diagonal values.

References

- [1] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349
- [2] Gill, P. E.; Murray, W. & Wright, M. H., Practical optimization, Academic press, 1981

```
matrix.approximation.positive_semidefinite.GMW_T2(A, min_diag_B=None,
                                                    max_diag_B=None,
                                                    min_diag_D=None, over-
                                                    write_A=False)
```

Computes a positive definite approximation of *A*.

Returns *A* if *A* is positive definite and meets the constrains and otherwise a positive definite approximation of *A*.

Parameters

- **A** (`numpy.ndarray`) – The matrix that should be approximated. *A* must be symmetric.
- **min_diag_B** (`numpy.ndarray` or `float`) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (`numpy.ndarray` or `float`) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (`float`) – Each component of the diagonal of the matrix *D* in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns *B* – An approximation of *A* which is positive definite.

Return type `numpy.ndarray`

Raises `matrix.errors.MatrixNotSquareError` – If *A* is not a square matrix.

Notes

The algorithm is introduced in [1]. This discription has been used for this implementation. The algorithm is based on [2]. The implementation has been extended to allow restrictions on the diagonal values.

References

- [1] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349
- [2] Gill, P. E.; Murray, W. & Wright, M. H., Practical optimization, Academic press, 1981

```
matrix.approximation.positive_semidefinite.SE_90(A, min_diag_B=None,
max_diag_B=None,
min_diag_D=None, over-
write_A=False)
```

Computes a positive definite approximation of A .

Returns A if A is positive definite and meets the constrains and otherwise a positive definite approximation of A .

Parameters

- **A** (*numpy.ndarray*) – The matrix that should be approximated. A must be symmetric.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix D in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A . Enabling may result in performance gain. optional, default: False

Returns B – An approximation of A which is positive definite.

Return type *numpy.ndarray*

Raises *matrix.errors.MatrixNotSquareError* – If A is not a square matrix.

Notes

The algorithm is introduced in [1]. Is is also described in [2]. This discription has been used for this implementation. The implementation has been extended to allow restrictions on the diagonal values.

References

- [1] Schnabel, R. & Eskow, E., A New Modified Cholesky Factorization, SIAM Journal on Scientific and Statistical Computing, 1990, 11, 1136-1158
- [2] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349

```
matrix.approximation.positive_semidefinite.SE_99(A, min_diag_B=None,
max_diag_B=None,
min_diag_D=None, over-
write_A=False)
```

Computes a positive definite approximation of A .

Returns A if A is positive definite and meets the constrains and otherwise a positive definite approximation of A .

Parameters

- **A** (*numpy.ndarray*) – The matrix that should be approximated. *A* must be symmetric.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.
- **max_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns B – An approximation of *A* which is positive definite.

Return type *numpy.ndarray*

Raises *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.

Notes

The algorithm is introduced in [1]. Is is also described in [2]. This discription has been used for this implementation. The algorithm is based on [3]. The implementation has been extended to allow restrictions on the diagonal values.

References

- [1] Schnabel, R. & Eskow, E., A Revised Modified Cholesky Factorization Algorithm, SIAM Journal on Optimization, 1999, 9, 1135-1148
- [2] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349
- [3] Schnabel, R. & Eskow, E., A New Modified Cholesky Factorization, SIAM Journal on Scientific and Statistical Computing, 1990, 11, 1136-1158

```
matrix.approximation.positive_semidefinite.SE_T1(A, min_diag_B=None,
max_diag_B=None,
min_diag_D=None,
write_A=False)
```

Computes a positive definite approximation of *A*.

Returns *A* if *A* is positive definite and meets the constrains and otherwise a positive definite approximation of *A*.

Parameters

- **A** (*numpy.ndarray*) – The matrix that should be approximated. *A* must be symmetric.
- **min_diag_B** (*numpy.ndarray* or *float*) – Each component of the diagonal of the returned matrix is forced to be greater or equal to *min_diag_B*. optional, default : No minimal value is forced.

- **max_diag_B** (*numpy.ndarray or float*) – Each component of the diagonal of the returned matrix is forced to be lower or equal to *max_diag_B*. optional, default : No maximal value is forced.
- **min_diag_D** (*float*) – Each component of the diagonal of the matrix *D* in a LDL^T decomposition of the returned matrix is forced to be greater or equal to *min_diag_D*. *min_diag_D* must be positive. optional, default : Is chosen by the algorithm.
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite *A*. Enabling may result in performance gain. optional, default: False

Returns **B** – An approximation of *A* which is positive definite.

Return type *numpy.ndarray*

Raises *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.

Notes

The algorithm is introduced in [1]. This discription has been used for this implementation. The algorithm is based on [2]. The implementation has been extended to allow restrictions on the diagonal values.

References

- [1] Fang, H.-r. & O’Leary, D. P., Modified Cholesky algorithms: a catalog with new approaches, Mathematical Programming, 2008, 115, 319-349
- [2] Schnabel, R. & Eskow, E., A Revised Modified Cholesky Factorization Algorithm, SIAM Journal on Optimization, 1999, 9, 1135-1148
- [3] Schnabel, R. & Eskow, E., A New Modified Cholesky Factorization, SIAM Journal on Scientific and Statistical Computing, 1990, 11, 1136-1158

4.1.2 Nearest matrix with specific properties

This module provides functions to compute matrices with minimal difference to an input matrix and specific properties.

`matrix.nearest.correlation_matrix(A, max_iterations=1000)`

Computes a correlation matrix closest to *A* in the Frobenius norm. A correlation matrix is a positive semidefinite matrix with ones on the diagonal.

Parameters

- **A** (*numpy.ndarray*) – *A* must be Hermitian.
- **max_iterations** (*int*) – The maximal number of iterations used for the calculation.

Returns **B** – A correlation matrix closest to *A* in the Frobenius norm.

Return type *numpy.ndarray*

Raises *TooManyIterationsError* – If the computation needs more iterations than the maximal number of iterations.

Notes

The method is presented in [1]. For the computation some code of Michael Croucher is used. See this source code for the license.

References

- [1] **Higham, N. J.** Computing the Nearest Correlation Matrix—A Problem from Finance IMA J. Numer. Anal., 2002, 22, 329-343

`matrix.nearest.positive_semidefinite_matrix(A, symmetric=False)`

Computes a symmetric positive semidefinite matrix with minimal difference to A in the Frobenius norm.

Parameters

- **A** (`numpy.ndarray`) – A must be Hermitian.
- **symmetric** (`bool`) – Whether A can be assumed to be symmetric or not. optional, default: False

Returns B – A symmetric positive semidefinite Hermitian matrix with minimal difference to A in the Frobenius norm.

Return type `numpy.ndarray`

Notes

The method is presented in [1].

References

- [1] **Higham, N. J.** Computing a nearest symmetric positive semidefinite matrix Linear Algebra and its Applications, 1988, 103, 103-118

`matrix.nearest.skew_symmetric_matrix(A)`

Computes a skew-symmetric matrix with minimal difference to A for any unitarily invariant norm.

Parameters A (`numpy.ndarray`) – A must be a square matrix.

Returns B – A skew-symmetric matrix with minimal difference to A for any unitarily invariant norm.

Return type `numpy.ndarray`

`matrix.nearest.symmetric_matrix(A)`

Computes a symmetric matrix with minimal difference to A for any unitarily invariant norm.

Parameters A (`numpy.ndarray`) – A must be a square matrix.

Returns B – A symmetric matrix with minimal difference to A for any unitarily invariant norm.

Return type `numpy.ndarray`

Notes

The optimality is proven in [1].

References

- [1] Fan, K., & Hoffman, A. (1955). Some Metric Inequalities in the Space of Matrices. Proceedings of the American Mathematical Society, 6(1), 111-116. doi:10.2307/2032662

4.1.3 Decompose a matrix

`matrix.decompose(A, permutation=None, return_type=None, check_finite=True, overwrite_A=False)`
Computes a decomposition of a matrix.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Matrix to be decomposed. A must be Hermitian.
- **permutation** (*str* or *numpy.ndarray*) – The symmetric permutation method that is applied to the matrix before it is decomposed. It has to be a value in *matrix.UNIVERSAL_PERMUTATION_METHODS*. If A is sparse, it can also be a value in *matrix.SPARSE_ONLY_PERMUTATION_METHODS*. It is also possible to directly pass a permutation vector. optional, default: no permutation
- **return_type** (*str*) – The type of the decomposition that should be calculated. It has to be a value in *matrix.DECOMPOSITION_TYPES*. If return_type is None the type of the returned decomposition is chosen by the function itself. optional, default: the type of the decomposition is chosen by the function itself
- **check_finite** (*bool*) – Whether to check that A contains only finite numbers. Disabling may result in problems (crashes, non-termination) if the inputs do contain infinities or NaNs. Disabling gives a performance gain. optional, default: True
- **overwrite_A** (*bool*) – Whether it is allowed to overwrite A. Enabling may result in performance gain. optional, default: False

Returns A decomposition of A of type *return_type*.

Return type *matrix.decompositions.DecompositionBase*

Raises

- *matrix.errors.NoDecompositionPossibleError* – If the decomposition of A is not possible.
- *matrix.errors.MatrixNotSquareError* – If A is not a square matrix.
- *matrix.errors.MatrixNotFiniteError* – If A is not a finite matrix and *check_finite* is True.

`matrix.UNIVERSAL_PERMUTATION_METHODS = ('none', 'decreasing_diagonal_values', 'increasing_diagonal_values')`
Supported permutation methods for decompose dense and sparse matrices.

`matrix.SPARSE_ONLY_PERMUTATION_METHODS = ()`
Supported permutation methods only for sparse matrices.

`matrix.DECOMPOSITION_TYPES = ('LDL', 'LDL_compressed', 'LL')`
Supported types of decompositions.

4.1.4 Examine a matrix

`matrix.is_positive_semidefinite(A, check_finite=True)`
Returns whether the passed matrix is positive semi-definite.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. *A* must be Hermitian.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive semi-definite.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If *A* is not a finite matrix and *check_finite* is True.

`matrix.is_positive_definite(A, check_finite=True)`

Returns whether the passed matrix is positive definite.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. *A* must be Hermitian.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is positive definite.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If *A* is not a finite matrix and *check_finite* is True.

`matrix.is_invertible(A, check_finite=True)`

Returns whether the passed matrix is an invertible matrix.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. *A* must be Hermitian and positive semidefinite.
- **check_finite** (*bool*) – Whether to check that *A* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns Whether *A* is invertible.

Return type `bool`

Raises `matrix.errors.MatrixNotFiniteError` – If *A* is not a finite matrix and *check_finite* is True.

4.1.5 Solve system of linear equations

`matrix.solve(A, b, overwrite_b=False, check_finite=True)`

Solves the equation $Ax = b$ regarding *x*.

Parameters

- **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be checked. *A* must be Hermitian and positive definite.

- **b** (*numpy.ndarray*) – Right-hand side vector or matrix in equation $Ax = b$. It must hold $b.shape[0] == A.shape[0]$.
- **overwrite_b** (*bool*) – Allow overwriting data in *b*. Enabling gives a performance gain. optional, default: False
- **check_finite** (*bool*) – Whether to check that *A* and *b* contain only finite numbers. Disabling may result in problems (crashes, non-termination) if they contain infinities or NaNs. Disabling gives a performance gain. optional, default: True

Returns An x so that $Ax = b$. The shape of x matches the shape of b .

Return type *numpy.ndarray*

Raises

- *matrix.errors.MatrixNotSquareError* – If *A* is not a square matrix.
- *matrix.errors.MatrixNotFiniteError* – If *A* is not a finite matrix and *check_finite* is True.
- *matrix.errors.MatrixSingularError* – If *A* is singular.

4.2 Matrix decompositions

Several matrix decompositions are supported. They are available in *matrix.decompositions*:

4.2.1 LL decomposition

class *matrix.decompositions.LL_Decomposition* (*L=None, p=None*)

Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. This decomposition is also called Cholesky decomposition.

Parameters

- **L** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix *L* of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where *A* is a matrix. optional, default: no permutation

L

The matrix *L* of the decomposition.

Type *numpy.matrix* or *scipy.sparse.spmatrix*

P

The permutation matrix. $P @ A @ P.T$ is the matrix *A* permuted by the permutation of the decomposition

Type *scipy.sparse.dok_matrix*

append_block_decomposition (*dec*)

Makes a new decomposition where this decomposition and the passed one are appended.

Parameters **dec** (*DecompositionBase*) – The decomposition that should be appended to this decomposition.

Returns **dec** – A new decomposition where this decomposition and the passed one are appended. This decomposition represents the first block and the passed one the second block.

Return type *DecompositionBase*

as_LDL_Decomposition ()

as_any_type (**type_strs*, *copy=False*)

Converts this decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_same_type (*dec*, *copy=False*)

Converts the passed decompositions to the same type as this decomposition.

Parameters

- **dec** (*DecompositionBase*) – The decomposition that should be converted.
- **copy** (*bool*) – Whether the data of the decomposition that should be converted should always be copied or only if needed.

Returns If the type of the passed decomposition is not same type as this decomposition, a decomposition of this type is returned which represents the same decomposed matrix as the passed decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type (*type_str*, *copy=False*)

Converts this decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible()

Check if this is a decomposition representing an invertible matrix.

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

composed_matrix

The composed matrix represented by this decomposition.

Type `numpy.matrix` or `scipy.sparse.spmatrix`

copy()

Copies this decomposition.

Returns A copy of this decomposition.

Return type `matrix.decompositions.DecompositionBase`

inverse_matrix_both_sides_multiplication(*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == x.shape[0]`.
- **y** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product $y.H @ B @ x$. It must hold `self.n == y.shape[0]`. optional, default: If *y* is not passed, *x* is used as *y*.
- **dtype** (`numpy.dtype`) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication(*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold `self.n == x.shape[0]`.
- **dtype** (`numpy.dtype`) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

is_almost_equal(*other*, *rtol=0.0001*, *atol=1e-06*)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.

- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

Whether this is a decompositon with permutation.

Type `bool`

is_positive_definite ()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite ()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular ()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse ()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type (*type_str*)

Whether this decomposition is of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load (*filename*)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises

- `FileNotFoundError` – If the files are not found in the passed directory.
- `DecompositionInvalidDecompositionTypeFile` – If the files contains another decomposition type.

matrix_both_sides_multiplication (*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == y.shape[0]`. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold `self.n == x.shape[0]`.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n

The dimension of the squared decomposed matrix.

Type `int`

p

The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

Type `numpy.ndarray`

p_inverse

The permutation vector that undoes the permutation.

Type `numpy.ndarray`

permute_matrix (*A*)

Permutes a matrix by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.

Returns The matrix *A* permuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve (*b*, *dtype=None*)

Solves the equation $Ax = b$ regarding *x*, where *A* is the composed matrix represented by this decomposition.

Parameters

- **b** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Right-hand side vector or matrix in equation $Ax = b$. It must hold `self.n == b.shape[0]`.
- **dtype** (`numpy.dtype`) – Type to use in computation. optional, default: Determined by the method.

Returns An *x* so that $Ax = b$. The shape of *x* matches the shape of *b*.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

type_str = `'LL'`

The type of this decomposition represented as string.

Type `str`

unpermute_matrix (*A*)

Unpermutes a matrix permuted by the permutation of the decomposition.

Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

4.2.2 LDL decomposition

class `matrix.decompositions.LDL_Decomposition` (*L=None*, *d=None*, *p=None*)

Bases: `matrix.decompositions.DecompositionBase`

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. *D* is a diagonal matrix. Only the diagonal values of *D* are stored.

Parameters

- **L** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix *L* of the decomposition. optional, If it is not set yet, it must be set later.

- **d** (*numpy.ndarray*) – The vector of the diagonal components of D of the decomposition. optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

D

The permutation matrix.

Type `scipy.sparse.dia_matrix`

L

The matrix L of the decomposition.

Type `numpy.matrix` or `scipy.sparse.spmatrix`

LD

A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

Type `numpy.matrix` or `scipy.sparse.spmatrix`

P

The permutation matrix. $P @ A @ P.T$ is the matrix A permuted by the permutation of the decomposition

Type `scipy.sparse.dok_matrix`

append_block_decomposition (*dec*)

Makes a new decomposition where this decomposition and the passed one are appended.

Parameters **dec** (*DecompositionBase*) – The decomposition that should be appended to this decomposition.

Returns **dec** – A new decomposition where this decomposition and the passed one are appended. This decomposition represents the first block and the passed one the second block.

Return type *DecompositionBase*

as_LDL_DecompositionCompressed ()**as_LL_Decomposition** ()**as_any_type** (**type_strs*, *copy=False*)

Converts this decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_same_type (*dec*, *copy=False*)

Converts the passed decompositions to the same type as this decomposition.

Parameters

- **dec** (*DecompositionBase*) – The decomposition that should be converted.

- **copy** (*bool*) – Whether the data of the decomposition that could be converted should always be copied or only if needed.

Returns If the type of the passed decomposition is not same type as this decomposition, a decomposition of this type is returned which represents the same decomposed matrix as the passed decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

as_type (*type_str*, *copy=False*)

Converts this decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix

The composed matrix represented by this decomposition.

Type *numpy.matrix* or *scipy.sparse.spmatrix*

copy ()

Copies this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

d

The diagonal vector of the matrix *D* of the decomposition.

Type *numpy.ndarray*

inverse_matrix_both_sides_multiplication (*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold *self.n == x.shape[0]*.

- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication (*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold $self.n == x.shape[0]$.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $B @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

is_almost_equal (*other*, *rtol=0.0001*, *atol=1e-06*)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type *bool*

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type *bool*

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type *bool*

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

Whether this is a decompositon with permutation.

Type `bool`

is_positive_definite()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type(type_str)

Whether this decomposition is of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(filename)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises

- `FileNotFoundError` – If the files are not found in the passed directory.
- `DecompositionInvalidDecompositionTypeFile` – If the files contains another decomposition type.

matrix_both_sides_multiplication (*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold `self.n == x.shape[0]`.

- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

matrix_right_side_multiplication (*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold $self.n == x.shape[0]$.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

n

The dimension of the squared decomposed matrix.

Type *int*

P

The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

Type *numpy.ndarray*

p_inverse

The permutation vector that undoes the permutation.

Type *numpy.ndarray*

permute_matrix (A)

Permutes a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

save (*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve (b , *dtype=None*)

Solves the equation $A x = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters

- **b** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation $A x = b$. It must hold $self.n == b.shape[0]$.

- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns An x so that $Ax = b$. The shape of x matches the shape of b .

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'LDL'

The type of this decomposition represented as string.

Type *str*

unpermute_matrix (A)

Unpermutes a matrix permuted by the permutation of the decomposition.

Parameters A (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix A unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

4.2.3 LDL decomposition compressed

class *matrix.decompositions.LDL_DecompositionCompressed* ($LD=None, p=None$)

Bases: *matrix.decompositions.DecompositionBase*

A matrix decomposition where LDL^H is the decomposed (permuted) matrix.

L is a lower triangle matrix with ones on the diagonal. D is a diagonal matrix. L and D are stored in one matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

Parameters

- **LD** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L . optional, If it is not set yet, it must be set later.
- **p** (*numpy.ndarray*) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

D

The permutation matrix.

Type *scipy.sparse.dia_matrix*

L

The matrix L of the decomposition.

Type *numpy.matrix* or *scipy.sparse.spmatrix*

LD

A matrix whose diagonal values are the diagonal values of D and whose off-diagonal values are those of L .

Type *numpy.matrix* or *scipy.sparse.spmatrix*

P

The permutation matrix. $P @ A @ P.T$ is the matrix A permuted by the permutation of the decomposition

Type `scipy.sparse.dok_matrix`

append_block_decomposition (*dec*)

Makes a new decomposition where this decomposition and the passed one are appended.

Parameters *dec* (`DecompositionBase`) – The decomposition that should be appended to this decomposition.

Returns *dec* – A new decomposition where this decomposition and the passed one are appended. This decomposition represents the first block and the passed one the second block.

Return type `DecompositionBase`

as_LDL_Decomposition ()

as_any_type (**type_strs*, *copy=False*)

Converts this decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

as_same_type (*dec*, *copy=False*)

Converts the passed decompositions to the same type as this decomposition.

Parameters

- **dec** (`DecompositionBase`) – The decomposition that should be converted.
- **copy** (*bool*) – Whether the data of the decomposition that could be converted should always be copied or only if needed.

Returns If the type of the passed decomposition is not same type as this decomposition, a decomposition of this type is returned which represents the same decomposed matrix as the passed decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

as_type (*type_str*, *copy=False*)

Converts this decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix

The composed matrix represented by this decomposition.

Type *numpy.matrix* or *scipy.sparse.spmatrix*

copy ()

Copies this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

d

The diagonal vector of the matrix *D* of the decomposition.

Type *numpy.ndarray*

inverse_matrix_both_sides_multiplication (*x, y=None, dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == x.shape[0]$.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == y.shape[0]$. optional, default: If *y* is not passed, *x* is used as *y*.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication (*x, dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where *B* is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold $self.n == x.shape[0]$.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

is_almost_equal (*other*, *rtol*=0.0001, *atol*=1e-06)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

Whether this is a decomposition with permutation.

Type `bool`

is_positive_definite ()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite ()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular ()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type(*type_str*)

Whether this decomposition is of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(*filename*)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises

- `FileNotFoundError` – If the files are not found in the passed directory.
- `DecompositionInvalidDecompositionTypeFile` – If the files contains another decomposition type.

matrix_both_sides_multiplication (*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold $self.n == x.shape[0]$.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold $self.n == x.shape[0]$.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

n
The dimension of the squared decomposed matrix.
Type `int`

P
The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition
Type `numpy.ndarray`

p_inverse
The permutation vector that undoes the permutation.
Type `numpy.ndarray`

permute_matrix (A)
Permutes a matrix by the permutation of the decomposition.
Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be permuted.
Returns The matrix A permuted by the permutation of the decomposition.
Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

save (*filename*)
Saves this decomposition.
Parameters **filename** (*str*) – Where this decomposition should be saved.

solve (b , *dtype=None*)
Solves the equation $Ax = b$ regarding x , where A is the composed matrix represented by this decomposition.
Parameters

- **b** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Right-hand side vector or matrix in equation $Ax = b$. It must hold $self.n == b.shape[0]$.
- **dtype** (`numpy.dtype`) – Type to use in computation. optional, default: Determined by the method.

Returns An x so that $Ax = b$. The shape of x matches the shape of b .
Return type `numpy.ndarray` or `scipy.sparse.spmatrix`
Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

type_str = 'LDL_compressed'
The type of this decomposition represented as string.
Type `str`

unpermute_matrix (A)
Unpermutes a matrix permuted by the permutation of the decomposition.
Parameters **A** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – The matrix that should be unpermuted.
Returns The matrix A unpermuted by the permutation of the decomposition.
Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

4.2.4 Base decomposition

class `matrix.decompositions.DecompositionBase` (*p=None*)

Bases: `object`

A matrix decomposition.

This class is a base class for all other matrix decompositions.

Parameters *p* (`numpy.ndarray`) – The permutation vector used for the decomposition. This decomposition is of $A[p[:, np.newaxis], p[np.newaxis, :]]$ where A is a matrix. optional, default: no permutation

P

The permutation matrix. $P @ A @ P.T$ is the matrix A permuted by the permutation of the decomposition

Type `scipy.sparse.dok_matrix`

append_block_decomposition (*dec*)

Makes a new decomposition where this decomposition and the passed one are appended.

Parameters *dec* (`DecompositionBase`) – The decomposition that should be appended to this decomposition.

Returns *dec* – A new decomposition where this decomposition and the passed one are appended. This decomposition represents the first block and the passed one the second block.

Return type `DecompositionBase`

as_any_type (**type_strs, copy=False*)

Converts this decomposition to any of the passed types.

Parameters

- ***type_strs** (*str*) – The decomposition types to any of them this this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not in *type_strs*, a decomposition of type *type_str[0]* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

as_same_type (*dec, copy=False*)

Converts the passed decompositions to the same type as this decomposition.

Parameters

- **dec** (`DecompositionBase`) – The decomposition that should be converted.
- **copy** (*bool*) – Whether the data of the decomposition that could be converted should always be copied or only if needed.

Returns If the type of the passed decomposition is not same type as this decomposition, a decomposition of this type is returned which represents the same decomposed matrix as the passed decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type `matrix.decompositions.DecompositionBase`

as_type (*type_str, copy=False*)

Converts this decomposition to passed type.

Parameters

- **type_str** (*str*) – The decomposition type to which this decomposition is converted.
- **copy** (*bool*) – Whether the data of this decomposition should always be copied or only if needed.

Returns If the type of this decomposition is not *type_str*, a decomposition of type *type_str* is returned which represents the same decomposed matrix as this decomposition. Otherwise this decomposition or a copy of it is returned, depending on *copy*.

Return type *matrix.decompositions.DecompositionBase*

check_finite (*check_finite=True*)

Check if this is a decomposition representing a finite matrix.

Parameters **check_finite** (*bool*) – Whether to perform this check. default: True

Raises *matrix.errors.DecompositionNotFiniteError* – If this is a decomposition representing a non-finite matrix.

check_invertible ()

Check if this is a decomposition representing an invertible matrix.

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

composed_matrix

The composed matrix represented by this decomposition.

Type *numpy.matrix* or *scipy.sparse.spmatrix*

copy ()

Copies this decomposition.

Returns A copy of this decomposition.

Return type *matrix.decompositions.DecompositionBase*

inverse_matrix_both_sides_multiplication (*x, y=None, dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == x.shape[0]$.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ B @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

inverse_matrix_right_side_multiplication (*x, dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $B @ x$, where B is the matrix inverse of the composed matrix represented by this decomposition.

Parameters

- **x** (`numpy.ndarray` or `scipy.sparse.spmatrix`) – Vector or matrix in the product in the matrix-matrix or matrix-vector $B @ x$. It must hold `self.n == x.shape[0]`.
- **dtype** (`numpy.dtype`) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $B @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

Raises `matrix.errors.DecompositionSingularError` – If this is a decomposition representing a singular matrix.

is_almost_equal (*other*, *rtol*=0.0001, *atol*=1e-06)

Whether this decomposition is close to passed decomposition.

Parameters

- **other** (*str*) – The decomposition which to compare to this decomposition.
- **rtol** (*float*) – The relative tolerance parameter.
- **atol** (*float*) – The absolute tolerance parameter.

Returns Whether this decomposition is close to passed decomposition.

Return type `bool`

is_equal (*other*)

Whether this decomposition is equal to passed decomposition.

Parameters **other** (*str*) – The decomposition which to compare to this decomposition.

Returns Whether this decomposition is equal to passed decomposition.

Return type `bool`

is_finite ()

Returns whether this is a decomposition representing a finite matrix.

Returns Whether this is a decomposition representing a finite matrix.

Return type `bool`

is_invertible ()

Returns whether this is a decomposition representing an invertible matrix.

Returns Whether this is a decomposition representing an invertible matrix.

Return type `bool`

is_permuted

Whether this is a decompositon with permutation.

Type `bool`

is_positive_definite ()

Returns whether this is a decomposition of a positive definite matrix.

Returns Whether this is a decomposition of a positive definite matrix.

Return type `bool`

is_positive_semidefinite ()

Returns whether this is a decomposition of a positive semi-definite matrix.

Returns Whether this is a decomposition of a positive semi-definite matrix.

Return type `bool`

is_singular()

Returns whether this is a decomposition representing a singular matrix.

Returns Whether this is a decomposition representing a singular matrix.

Return type `bool`

is_sparse()

Returns whether this is a decomposition of a sparse matrix.

Returns Whether this is a decomposition of a sparse matrix.

Return type `bool`

is_type(type_str)

Whether this decomposition is of the passed type.

Parameters **type_str** (*str*) – The decomposition type according to which is checked.

Returns Whether this is a decomposition of the passed type.

Return type `bool`

load(filename)

Loads a decomposition of this type.

Parameters **filename** (*str*) – Where the decomposition is saved.

Raises

- `FileNotFoundError` – If the files are not found in the passed directory.
- `DecompositionInvalidDecompositionTypeFile` – If the files contains another decomposition type.

matrix_both_sides_multiplication (*x*, *y=None*, *dtype=None*)

Calculates the both sides (matrix-matrix or matrix-vector) product $y.H @ A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold $self.n == x.shape[0]$.
- **y** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product $y.H @ A @ x$. It must hold $self.n == y.shape[0]$. optional, default: If y is not passed, x is used as y.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $y.H @ A @ x$.

Return type `numpy.ndarray` or `scipy.sparse.spmatrix`

matrix_right_side_multiplication (*x*, *dtype=None*)

Calculates the right side (matrix-matrix or matrix-vector) product $A @ x$, where A is the composed matrix represented by this decomposition.

Parameters

- **x** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Vector or matrix in the product in the matrix-matrix or matrix-vector $A @ x$. It must hold $self.n == x.shape[0]$.

- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns The result of $A @ x$.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

n

The dimension of the squared decomposed matrix.

Type *int*

P

The permutation vector. $A[p[:, np.newaxis], p[np.newaxis, :]]$ is the matrix A permuted by the permutation of the decomposition

Type *numpy.ndarray*

p_inverse

The permutation vector that undoes the permutation.

Type *numpy.ndarray*

permute_matrix (A)

Permutes a matrix by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be permuted.

Returns The matrix A permuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

save (*filename*)

Saves this decomposition.

Parameters **filename** (*str*) – Where this decomposition should be saved.

solve (b , *dtype=None*)

Solves the equation $A x = b$ regarding x , where A is the composed matrix represented by this decomposition.

Parameters

- **b** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – Right-hand side vector or matrix in equation $A x = b$. It must hold $self.n == b.shape[0]$.
- **dtype** (*numpy.dtype*) – Type to use in computation. optional, default: Determined by the method.

Returns An x so that $A x = b$. The shape of x matches the shape of b .

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

Raises *matrix.errors.DecompositionSingularError* – If this is a decomposition representing a singular matrix.

type_str = 'base'

The type of this decomposition represented as string.

Type *str*

unpermute_matrix (A)

Unpermutes a matrix permuted by the permutation of the decomposition.

Parameters **A** (*numpy.ndarray* or *scipy.sparse.spmatrix*) – The matrix that should be unpermuted.

Returns The matrix *A* unpermuted by the permutation of the decomposition.

Return type *numpy.ndarray* or *scipy.sparse.spmatrix*

4.3 Errors

This is an overview about the exceptions that could arise in this library. They are available in *matrix.errors*:

The following exception is the base exception from which all other exceptions in this package are derived:

4.3.1 BaseError

exception *matrix.errors.BaseError* (*message*)

Bases: *Exception*

This is the base exception for all exceptions in this package.

If a matrix has an invalid properties, the following exceptions can occur:

4.3.2 MatrixError

exception *matrix.errors.MatrixError* (*matrix*, *message=None*)

Bases: *matrix.errors.BaseError*

An exception related to a matrix.

4.3.3 MatrixNotSquareError

exception *matrix.errors.MatrixNotSquareError* (*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix is not a square matrix although a square matrix is required.

4.3.4 MatrixNotFiniteError

exception *matrix.errors.MatrixNotFiniteError* (*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix has non-finite entries although a finite matrix is required.

4.3.5 MatrixSingularError

exception *matrix.errors.MatrixSingularError* (*matrix*)

Bases: *matrix.errors.MatrixError*

A matrix is singular although an invertible matrix is required.

4.3.6 MatrixNotHermitianError

exception `matrix.errors.MatrixNotHermitianError` (*matrix, i=None, j=None*)
Bases: `matrix.errors.MatrixError`

A matrix is not Hermitian although a Hermitian matrix is required.

4.3.7 MatrixComplexDiagonalValueError

exception `matrix.errors.MatrixComplexDiagonalValueError` (*matrix, i=None*)
Bases: `matrix.errors.MatrixNotHermitianError`

A matrix has complex diagonal values although real diagonal values are required.

If a desired decomposition is not computable, the following exceptions can be raised:

4.3.8 NoDecompositionPossibleError

exception `matrix.errors.NoDecompositionPossibleError` (*base, desired_type*)
Bases: `matrix.errors.BaseError`

It is not possible to calculate a desired matrix decomposition.

4.3.9 NoDecompositionPossibleWithProblematicSubdecompositionError

exception `matrix.errors.NoDecompositionPossibleWithProblematicSubdecompositionError` (*base, desired_type, problematic_subdecomposition=Non*)
Bases: `matrix.errors.NoDecompositionPossibleError`

It is not possible to calculate a desired matrix decomposition. Only a subdecomposition could be calculated

4.3.10 NoDecompositionPossibleTooManyEntriesError

exception `matrix.errors.NoDecompositionPossibleTooManyEntriesError` (*matrix, desired_type*)
Bases: `matrix.errors.NoDecompositionPossibleError`

The decomposition is not possible for this matrix because it would have too many entries.

4.3.11 NoDecompositionConversionImplementedError

exception `matrix.errors.NoDecompositionConversionImplementedError` (*decomposition, desired_type*)

Bases: `matrix.errors.NoDecompositionPossibleError`

A decomposition conversion is not implemented for this type.

If the matrix, represented by a decomposition, has an invalid characteristic, the following exceptions can occur:

4.3.12 DecompositionError

exception `matrix.errors.DecompositionError` (*decomposition, message=None*)

Bases: `matrix.errors.BaseError`

An exception related to a decomposition.

4.3.13 DecompositionNotFiniteError

exception `matrix.errors.DecompositionNotFiniteError` (*decomposition*)

Bases: `matrix.errors.DecompositionError`

A decomposition of a matrix has non-finite entries although a finite matrix is required.

4.3.14 DecompositionSingularError

exception `matrix.errors.DecompositionSingularError` (*decomposition*)

Bases: `matrix.errors.DecompositionError`

A decomposition represents a singular matrix although a non-singular matrix is required.

If a decomposition could not be loaded from a file, the following exceptions can be raised:

4.3.15 DecompositionInvalidFile

exception `matrix.errors.DecompositionInvalidFile` (*filename*)

Bases: `matrix.errors.DecompositionError, OSError`

An attempt was made to load a decomposition from an invalid file.

4.3.16 DecompositionInvalidDecompositionTypeFile

exception `matrix.errors.DecompositionInvalidDecompositionTypeFile` (*filename, type_file, type_needed*)

Bases: `matrix.errors.DecompositionInvalidFile`

An attempt was made to load a decomposition from an file in which another decomposition type is stored.

If the computation needs more iterations than the maximal number of iterations, the following exception occurs:

4.3.17 TooManyIterationsError

exception `matrix.errors.TooManyIterationsError` (*message=None, iteration=None, result=None*)

Bases: `matrix.errors.BaseError`

Too many iterations are needed for the calculation.

4.4 Changelog

4.4.1 1.2

- Several functions to solve nearness problems (nearest symmetric matrix, nearest skew symmetric matrix, nearest positive semidefinite matrix, nearest correlation matrix) added.
- Significant speedup of approximation algorithms in `matrix.approximation.positive_semidefinite.Reimer`.
- Overflow handling improved in several functions.
- Decompositions in `matrix.decompositions` now have an `append_block_decomposition` and `as_same_type` method and their multiplication methods have now a `dtype` argument.
- The approximation algorithms in `matrix.approximation.positive_semidefinite.Reimer` now have a `min_abs_value_L` argument.

4.4.2 1.1

- Positive semidefinite approximation algorithms of GMW and SE type have been added.
- Permutation method, with numerical stability as main focus, has been added to positive semidefinite approximation algorithm.
- Positive semidefinite approximation algorithm are moved into separate package. (`matrix.approximate` to `matrix.approximation.positive_semidefinite`)

4.4.3 1.0.1

- Approximation functions now also work if an overflows occurs.
- NumPys matrix is avoided because it is deprecated now.

4.4.4 1.0

- Approximation functions are slightly faster now.
- Better overflow handling is now used in approximation functions.
- Prebuild html documentation are now included.
- Function for approximating a matrix by a positive semidefinite matrix (`matrix.approximate.positive_semidefinite_matrix`) has been removed.

4.4.5 0.8

- Approximation functions have been replaced by more sophisticated approximation functions.
- Explicit function for approximating a matrix by a positive (semi)definite matrix has been added.
- Universal save and load functions have been added.
- Decompositions have obtained `is_equal` and `is_almost_equal` methods.
- Functions to multiply the matrix, represented by a decomposition, or its inverse with a matrix or a vector have been added.
- It is now possible to pass permutation vectors to approximate and decompose methods.

4.4.6 0.7

- Lineare systems associated to matrices or decompositions can now be solved.
- Invertibility of matrices and decompositions can now be examined.
- Decompositions can now be examined to see if they contain only finite values.

4.4.7 0.6

- Decompositions are now saveable and loadable.

4.4.8 0.5

- Matrices can now be approximated by decompositions.

4.4.9 0.4

- Positive definiteness and positive semi-definiteness of matrices and decompositions can now be examined.

4.4.10 0.3

- Dense and sparse matrices are now decomposable into several types (LL, LDL, LDL compressed).

4.4.11 0.2

- Decompositons are now convertible to other decompositon types.
- Decompositions are now comparable.

4.4.12 0.1

- Several decompositions types (LL, LDL, LDL compressed) have been added.
- Several permutation capabilities have been added.

4.5 Requirements

- Python ≥ 3.7
- NumPy ≥ 1.15
- SciPy ≥ 0.19
- scikit-sparse $\geq 0.4.2$ (only for sparse matrix support)

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